



## Q.11-Q.35 carry one mark each.

11. Which of the following phase space plots is correct for the potential  $U(x) = -\frac{1}{2}x^3$ ?



- 12. A particle moves relative to O' with a constant velocity of  $\frac{c}{2}$  in the x'y'-plane such that its trajectory makes an angle of 60° with the *x*'-axis. If the velocity of O' with respect to O is 0.6*c* along the *x*-*x*' axis, the equations of motion of the particle as determined by O are
  - (a) x = 0.74ct, y = 0.30ct (b) x = 0.60ct, y = 0.70ct
  - (c) x = 0.37ct, y = 0.15ct (d) x = 0.90ct, y = 0.45ct
- 13. Consider two ultra-high speed drag racers. One drag racer has a red stripe on the side and overtaken the other drag racer at a relative speed of  $\sqrt{3}c/2$ . If the red stripe has wavelength 635 nm, then the wavelength of the stripe as observed by the other drag racer is \_\_\_\_\_ nm. (correct up to one decimal
- 15. Light of wavelength 4300Å is incident on a nickel surface of work function 5 electron volts and a potassium surface work function 2.3 electron volts. If the electron will be emitted, then max velocity of Ni and K is
  (a) 0, 1.423×10<sup>5</sup> m/s
  (b) 3.2×10<sup>5</sup> m/s, 0
  (c) 3.2×10<sup>5</sup> m/s, 1.423×10<sup>5</sup> m/s
  (d) In both cases electron will not be emitted.
- 16. If 15 electron in system of P.E. V(x, y), where  $V(x, y) = \frac{1}{2}mw^2(x^2 + y^2)$ . The degeneracy of most energetic electron is \_\_\_\_\_
- 17. Consider a system of two ising spin  $S_1$  and  $S_2$  taking value  $\pm 1$  with interaction energy,  $\in = -JS_1S_2$  in thermal equilibrium at temperature *T*. The number of configurations corresponding to ground state energy of the system is \_\_\_\_\_\_.



places)

2

- 18. For vaporization among the following which option is correct?
  - (a) Entropy and specific heat at constant pressure are discontinuous at transition point.
  - (b) Entropy and isothermal compressibility are discontinuous at transition point.
  - (c) Entropy, specific heat at constant and isothermal compressibility are discontinuous at transition point.
  - (d) Specific heat at constant pressure , isothermal compressibility and coefficient of volume expansion at constant pressure all are infinite at transition point.
- 19. For case of n = 2,  $\ell = 1$ , m = 0 the value of *r* at which the radial probability density of the hydrogen atom

reaches its maximum is 
$$a_0$$
. Given  $R_2$ ,  $(r) = \frac{1}{\left(2\sqrt{6} a_0^{5/2}\right)} re^{-r/2a_0}$ 

20. Consider a particle of mass *m*, moving in one-dimension whose wavefunction is given as following:

$$\psi(x) = \begin{cases} 2\alpha^{3/2} x e^{-\alpha x} & \text{for } x > 0\\ 0 & \text{for } x < 0 \end{cases}$$

The most probable position of the particle will be

- (a)  $\alpha$  (b)  $\frac{1}{\alpha}$  (c)  $\frac{1}{\sqrt{\alpha}}$  (d) 0
- 21. Let *P* be an n×n matrix with integral entries and  $Q = P + \frac{1}{2}I$ , where *I* denotes the *n*×*n* identity matrix, then *Q* 
  - is (a) idempotent (b) invertiple (c) nilpotent (d) unipotent
- 23. Consider a parallel plate capacitor of capacitance C. If a very thin conducting plated is inserted parallely in halfway between the plates, then the capacitance will be
  - (a) 2*C*

- (c) C (d) zero
- 24. A thin circular disc of radius *a* having surface charge density  $\sigma$  on it. If V(x) is the electrostatic potential  $d^{2}V(x)$

at an axial point *P* at a distance *x* from the centre of the disc, then the value of  $\frac{d^2 V(x)}{dx^2}\Big|_{x=0}$  is

- (a)  $\frac{\sigma}{2\varepsilon_0 a}$  (b)  $\frac{\sigma}{2\varepsilon_0}$  (c)  $-\frac{\sigma}{2\varepsilon_0}$  (d) infinity
- 25. Which of the following nuclear reactions is not forbidden?
  - (a)  $\Sigma^+ + n \to \Sigma^- + p$ (b)  $\pi^+ + n \to k^+ + k^+$ (c)  $\Lambda^0 \to p + e^- + \overline{v}_e$ (d)  $\mu^- \to e^- + \overline{v}_e + \overline{v}_\mu$
- 26. A pion decays from rest to give a muon of 3.57 MeV energy in a reaction,  $\pi^+ \rightarrow \mu^+ + v_{\mu}$ . The kinetic energy of the associated neutrino is \_\_\_\_\_\_MeV (upto two decimal places)

[Given :  $m_{\pi^+} = 273 m_e, m_{\mu^+} = 207 m_e$  and  $m_e = 0.51 MeV/c^2$ ]

(b)  $\frac{C}{2}$ 



- 27. A positive point charged particle moves with uniform velocity  $\overline{v} = 4\hat{i} m/\sec$  in a region where  $\vec{E} = 20 \hat{j} V/m$ and  $\vec{B} = B_0 \hat{k} W b/m^2$ . The value of  $B_0$  for which the velocity of the particle remains constant is \_\_\_\_\_\_W b/m^2 (answer should be an integer).
- 28. A uniform charged sphere of radius a and carrying the charge density  $\rho$  and spinning at a constant angular velocity  $\omega$  about *z*-axis. The current density at any point  $(r, \theta, \phi)$  inside the sphere is given by
  - (a)  $\rho \omega r \hat{\phi}$  (b)  $\rho \omega r \sin \theta \hat{\phi}$  (c)  $\rho \omega r \cos \theta \hat{\phi}$  (d)  $\rho \omega \cos \theta \hat{\phi}$
- 29. The gain of the circuit is \_\_\_\_\_\_ (upto first decimal places)



- 30.In a 4-bit D/A converter the full scale output voltage is 5V. Its resolution is approximately<br/>(a) 0.3 V(b) 1.25 V(c) 0.5 V(d) 2.5 V
- 31. In carbon atoms which of the following terms will have minimum energy

(a) 
$${}^{1}D_{2}$$
 (b)  ${}^{3}P_{2}$  (c)  ${}^{3}P_{0}$  (d)  ${}^{1}S_{0}$   
Which of the following molecule is rotational without and NMP setting?

- 32. Which of the following molecule is rotational, vibrational, Raman and NMR active? (a)  ${}^{12}C{}^{-16}O$ (b)  ${}^{1}H{}^{-1}H$ (c)  ${}^{1}H{}^{-35}Cl$ (d)  ${}^{6}C{}^{-16}N$
- 33. A two-dimensional lattice has basis vectors,  $a = 2\hat{i}$  and  $b = \hat{i} + 2\hat{j}$ . The basis vectors of the receiprocal lattice

(a) 
$$a^* = \pi \hat{i} - \frac{\pi}{2} \hat{j}$$
 and  $b^* = \pi \hat{j}$   
(b)  $a^* = \pi \hat{i} + \frac{\pi}{2} \hat{j}$  and  $b^* = \pi \hat{j}$   
(c)  $a^* = \pi \hat{i} - \frac{\pi}{2} \hat{j}$  and  $b^* = -\pi \hat{j}$   
(d)  $a^* = \pi \hat{i} + \frac{\pi}{2} \hat{j}$  and  $b^* = \frac{\pi}{2} \hat{j}$ 

- 34. According Josephson effect if we applied a static potential  $V_0$  across the junction it leads to production of alterneting current. If the value of  $V_0$  is 10 mvolt. The frequency of the current will be \_\_\_\_\_×10<sup>12</sup> Hz (answer should be upto second decimal place)
- 35. The length element *ds* of an arc is given by

$$(ds)^{2} = 3(dx^{1})^{2} + (dx^{2})^{2} + \sqrt{5}(dx^{1})(dx^{2})$$

The metric tensor  $g_{ij}$  is

(a) 
$$\begin{bmatrix} 3 & \sqrt{5} \\ \sqrt{5} & 1 \end{bmatrix}$$
 (b)  $\begin{bmatrix} 3 & \sqrt{5/4} \\ \sqrt{5/4} & 1 \end{bmatrix}$  (c)  $\begin{bmatrix} 3 & 0 \\ 0 & 1 \end{bmatrix}$  (d)  $\begin{bmatrix} 3 & \sqrt{5/2} \\ \sqrt{5/2} & 1 \end{bmatrix}$ 



## Q.36-Q.65 carry TWO marks each.

36. The Lagrangian of a system is given by

$$L = \frac{m}{2} (\dot{r}^2 + 4c^2 r^2 \dot{r}^2 + r^2 \omega^2) - mgcr^2$$

Where  $c, \omega, m$ , g are constants. The equation of motion of the system is

(a) 
$$\ddot{r} - \dot{r}^2 (4c^2r) + r(2gc - \omega^2) = 0$$
  
(b)  $\ddot{r} (1 + 4c^2r^2) - \dot{r}^2 (4c^2r) + r(2gc - \omega^2) = 0$   
(c)  $\ddot{r} (1 + 4c^2r^2) + \dot{r}^2 (4c^2r) + r(2gc - \omega^2) = 0$   
(d)  $\ddot{r} + \dot{r}^2 (4c^2r) + r(2gc - \omega^2) = 0$ 

37. A particle of mass *m* moves in one dimension under the influence of a force,  $F(x,t) = \frac{k}{x^2}e^{-(t/\tau)}$ 

Where k and  $\tau$  are positive constants. Then

- (a) Hamiltonian is not equal to the total energy and the total energy is not conserved.
- (b) Hamiltonian is equal to the total energy and the total energy is not conserved.
- (c) Hamiltonian is equal to the total energy and the total energy is conserved.
- (d) Hamiltonian is not equal to the total energy and the total energy is conserved.

38. A particle (mass m = 2 kg) at rest is attracted toward a center of force  $F = -\frac{mk^2}{x^3}$ , where  $k = 1 \text{ m}^2 \text{s}^{-1}$ . The time required to reach the force center from a distance 4 m is \_\_\_\_\_\_s.

- 39. Spacecraft A is moving at 0.90c with respect to the earth. If another spacecraft B is to pass A at a relative speed of 0.50c in the same direction, then the speed B must have (in units of *c*) with respect to the earth is \_\_\_\_\_\_ *c* (up to two decimal places).
- 40. In a one dimentional potential box of potential energy

$$V(x) = \begin{cases} 0 & -\frac{a}{4} < x < \frac{3a}{4} \\ \infty & \text{otherwise} \end{cases}$$

If its energy is  $\frac{2\pi^2\hbar^2}{ma^2}$  exist. Then the correct statement is **CAREER ENDEAVOUR** 

(a) 
$$\langle x \rangle = 0, \langle p \rangle = 0$$

(c) 
$$\langle x \rangle = \frac{a}{4}, \langle p \rangle = 0$$

(d) none of these

41. A particle is described by a wavefunction

$$\psi(x,\phi) = A e^{-r^2/2\Delta^2} \left(\frac{r}{\Delta}\cos\phi + \sin\phi\right)$$

If  $L_z$  is measured with result  $-\hbar$ , then the corresponding probability is \_\_\_\_\_

42. The Yukawa potential, 
$$V(r) = g \frac{e^{-\mu,r}}{r}$$
 with total energy E, where  $g = ze^2$  at  $\theta = \frac{\pi}{2}$  and  $\mu_0 = 0$ . The

differential scattering cross-section \_\_\_\_\_ 
$$\frac{(ze)}{(16E)}$$



For a particle of mass *m* moving in the potential  $V(x) = \frac{1}{2}m\omega^2 x^2$ , a small perturbation only for 43. positive x,  $H_p = \lambda x$  is applied with  $\lambda > 0$  constant. The first order correction to ground state energy is

6

44. A spin state precesses in a magnetic field same way as the classical magnetic dipole precesses in magnetic field with lasmor frequency given by  $\omega_L = -\gamma \vec{B}$ . consider the Hamiltonian  $\left(\gamma = g \frac{e}{2m}\right)$ 

$$\hat{H} = \frac{1}{2} \hbar \omega_0 \begin{pmatrix} 4 & 2+i \\ 2-i & 0 \end{pmatrix}$$

Calculate  $|\vec{\omega}_L|$  of the larmor frequency

- (b) 0(c)  $2\omega_{0}$ (d)  $3\omega_0$ (a)  $\omega_0$
- Two identical bodies have internal energy U = NCT, with a constant C. The values of N and C are same for 45. each body. The initial temperatures of the bodies are  $T_1$  and  $T_2$ , and they are used a source of work by connecting them to a Carnot heat engine and bringing them to a common final temperature T<sub>f</sub>. The work delivered is
  - (a) W = NC  $(T_1 + T_2)^2$ (b) W = NC  $(T_1 - T_2)^2$ (c) W = NC  $\left(\sqrt{T_1} - \sqrt{T_2}\right)^2$ (d) 0

46. The thermodynamics of a classical paramagnetic system are expressed by the variables: magnetization M, magnetic field B, and absolute temperature T. The equation of state is  $M = \frac{CB}{T}$ , where C = Curie constant.

The system's internal energy is:

U = -MB

VBEED The increment of the work done by the system upon the external environment is dW = MdB. The entropy of the system is given by

(a) 
$$S = S_0 - \frac{M^2}{2C}$$
 (b)  $S = S_0 - \frac{M}{C}$  (c)  $S = S_0 - 2MC$  (d)  $S = S_0$ 

Two thermally isolated identical systems have heat capacities which vary as  $C_v = \beta T^3$  (where  $\beta > 0$ ). Initially 47. one system is at 300K and the other at 400 K. The systems are then brought into thermal contact and the combined system is allowed to reach thermal equilibrium. The final temperature of the combined system is K.



48. The entropy of a gas containing *N* particles enclosed in a volume *V* is given by  $S = Nk_B \ln\left(\frac{aVE^{3/2}}{N^{5/2}}\right)$ , where

*E* is the total energy, *a* is constant and  $k_B$  is Boltzmann constant. The chemical potential  $\mu$  of the system at a temperature *T* is

(a) 
$$\mu = -k_B T \left[ \ln \left( \frac{a V E^{3/2}}{N^{5/2}} \right) \right]$$
  
(b)  $\mu = -k_B T \left[ \ln \left( \frac{a V E^{3/2}}{N^{5/2}} \right) - \frac{5}{2} \right]$   
(c)  $\mu = k_B T \left[ \ln \left( \frac{a V E^{3/2}}{N^{5/2}} \right) + \frac{5}{2} \right]$   
(d)  $\mu = k_B T \left[ \ln \left( \frac{a V E^{3/2}}{N^{5/2}} \right) \right]$ 

- 49. A 100 ohm resistor is held at a constant temperature of 300K. A current of 10 amperes is passed through the resistor for 300 sec. The change in entropy of the resistor is \_\_\_\_\_(J/K).
- 50. If  $y = \phi(x)$  is a particular solution of  $y'' + \sin x(y') + 2y = e^x$  and  $y = \psi(x)$  is a particular solution of  $y'' + \sin x(y') + 2y = \cos 2x$  then a particular solution of  $y'' + \sin x(y') + 2y = e^x + 2\sin^2 x$  is given by

(a) 
$$\phi(x) - \psi(x) + \frac{1}{2}$$
 (b)  $\psi(x) - \phi(x) + \frac{1}{2}$  (c)  $\phi(x) - \psi(x) + 1$  (d)  $\psi(x) - \phi(x) + 1$ 

51. If Y(p) is the laplace transform of y(t), which is the solution of the initial value problem

$$\frac{d^2 y}{dt^2} + y(t) = \begin{cases} 0 & 0 < t < 2\pi \\ \sin t & t > 2\pi \end{cases}$$

which y(0)=1 and y'(0)=0 the Y(p) equals

(a) 
$$\frac{p}{1+p^2} + \frac{e^{-2\pi p}}{\left(1+p^2\right)^{3/2}}$$
 (b)  $\frac{p+1}{1+p^2}$  (c)  $\frac{p}{1+p^2} + \frac{e^{-2p\pi}}{\left(1+p^2\right)}$  (d)  $\frac{p\left(1+p^2\right)+1}{\left(1+p^2\right)^2}$ 

- 52. Let  $A_1, A_2, \dots, A_n$  be *n* independent events which the probability of occurence of the event  $A_i$  given by  $P(A_i) = 1 - \frac{1}{\alpha^i}, \alpha > 1$ ,  $i = 1, 2, \dots, n$  then the probability that at least one the event occurs is (a)  $1 - \frac{1}{\alpha^{\frac{n(n+1)}{2}}}$  (b)  $\frac{1}{\alpha^{\frac{n(n+1)}{2}}}$  (c)  $\frac{1}{\alpha^n}$  (d)  $\left(1 - \frac{1}{\alpha^n}\right)$
- 53. Suppose a charge Q is distributed within a sphere of radius R in such a way that the charge density  $\rho(r)$  at a distance r from the center is

$$\rho(r) = \begin{cases} \frac{3Q}{\pi R^4} (R - r) & \text{for } 0 < r < R \\ 0 & \text{for } r > R \end{cases}$$

The value of maximum electric field due to this charge distribution is

(a) 
$$\frac{Q}{4\pi\varepsilon_0 R^2}$$
 (b)  $\frac{Q}{3\pi\varepsilon_0 R^2}$  (c)  $\frac{Q}{2\pi\varepsilon_0 R^2}$  (d)  $\frac{Q}{\pi\varepsilon_0 R^2}$ 



South Delhi : 28-A/11, Jia Sarai, Near-IIT Hauz Khas, New Delhi-16, Ph : 011-26851008, 26861009 North Delhi : 33-35, Mall Road, G.T.B. Nagar (Opp. Metro Gate No. 3), Delhi-09, Ph: 011-65462244, 65662255

- 54. The quardrupole moment for the ground state of  ${}_{8}O^{17}$  as given by single particle shell model is \_\_\_\_\_\_barn. (upto three decimal places) [Given : Radius  $R = R_0 A^{1/3}$  where  $R_0 = 1.2$  fermi ]
- 55. The binding energy of a nucleus with atomic number z and atomic mass number A is given by semi-empirical mass formula

$$B(z,A) = aA - bA^{2/3} - \frac{c(A-2z)^2}{A} - d\frac{z^2}{A^{1/3}} - \frac{\delta}{A^{1/2}}$$

where, a = 15.8 MeV, b = 18.3 MeV, c = 23.2 MeV, d = 0.7 MeV and  $\delta = (+11.2, 0, -11.2)$  MeV for nuclei which are (odd-odd, odd-even, even-even). If we consider all possible isobars of mass number 216, the most stable nuclei is

(a) 
$${}^{216}_{82}Pb$$
 (b)  ${}^{216}_{87}Fr$  (c)  ${}^{216}_{85}At$  (d)  ${}^{216}_{86}Rn$ 

56. Suppose a plane EM-wave with electric field

$$\vec{E} = \hat{x} 10 \cos(kz - \omega t) V m^{-1}$$

is incident from air on a dielelectric occupying the region  $z \ge 0$ . Assuming that the permittivity of the medium is  $4\varepsilon_0$  and permeability  $\mu_0$  the electric field of the reflected waves can be written as

- (a)  $\vec{E} = \hat{x} \frac{10}{3} \cos(kz \omega t)$ (b)  $\vec{E} = -\hat{x} \frac{10}{3} \cos(kz + \omega t)$ (c)  $\vec{E} = -\hat{x} \frac{10}{3} \cos(kz - \omega t)$ (d)  $\vec{E} = \hat{x} \frac{20}{3} \cos(kz - \omega t)$
- 57. Consider a dielectric-conductor interface at z = 0. The magnetic field in the dielectric  $z \le 0$  is given by  $\vec{H} = \hat{y}H_1 \cos kz \cos \omega t$ , then the surface current density is given by

(d)  $x^2 - 2y^2$ 

- (a)  $\hat{x}H_1 \sin \omega t$  (b)  $\hat{x}H_1 \cos \omega t$  (c)  $\hat{y}H_1 \sin \omega t$  (d)  $\hat{y} \cos \omega t$
- 58. Which of the following CANNOT BE the imaginary part of a complex analytic function f(z)?

(a) 
$$x^2 - y^2$$
 (b)  $x^3 - 3xy^2$  (c)  $x^3 - 3xy^2 + x$ 

59. The output of the given circuit is (assume that the diode is ideal)





South Delhi : 28-A/11, Jia Sarai, Near-IIT Hauz Khas, New Delhi-16, Ph : 011-26851008, 26861009 North Delhi : 33-35, Mall Road, G.T.B. Nagar (Opp. Metro Gate No. 3), Delhi-09, Ph: 011-65462244, 65662255 If the given circuit behave like mod-10 counter the inputs of NAND gate will be









South Delhi : 28-A/11, Jia Sarai, Near-IIT Hauz Khas, New Delhi-16, Ph : 011-26851008, 26861009

North Delhi : 33-35, Mall Road, G.T.B. Nagar (Opp. Metro Gate No. 3), Delhi-09, Ph: 011-65462244, 65662255

# PHYSICS-PH

### **GATE TEST SERIES-B**

Date: 14-01-2018

#### **ANSWER KEY**

1.	(b)	<b>2.</b> (a)	<b>3.</b> (c)	4.	(b)
5.	(c)	<b>6.</b> (b)	<b>7.</b> (b)	8.	(a)
9.	(b)	<b>10.</b> (b)	<b>11.</b> (c)	12.	(a)
13.	(317.5 to 317.9)	<b>14.</b> (26)	<b>15.</b> (a)	16.	(4)
17.	(2)	<b>18.</b> (d)	<b>19.</b> (4)	20.	(b)
21.	(c)	<b>22.</b> (-1)	<b>23.</b> (c)	24.	(d)
25.	(c)	<b>26.</b> (30.0 to 30.1)	<b>27.</b> (5)	28.	(b)
29.	(-1.5)	<b>30.</b> (a)	<b>31.</b> (c)	32.	(c)
33.	(a)	<b>34.</b> (4.8 to 4.89)	<b>35.</b> (b)	36.	(c)
37.	(b)	<b>38.</b> (16)	<b>39.</b> (0.96 to 0.98)		
40.	(c)	<b>41.</b> (0.5)	<b>42.</b> (0.5)	43.	(c)
44.	(d)	<b>45.</b> (c)	<b>46.</b> (a)	47.	(360.00 to 360.30)
48.	(b)	<b>49.</b> (0)	<b>50.</b> (a)	51.	(a)
52.	(a)	<b>53.</b> (b)	<b>54.</b> (0.031 to 0.03	4)	<b>55.</b> (c)
56.	(b)	<b>57.</b> (b)	<b>58.</b> (d)	59.	(b)
60.	(b)	<b>61.</b> (c)	<b>62.</b> (3)	63.	(6.2)
64.	(b)	<b>65.</b> (c)			

CAREER ENDEAVOUR



South Delhi : 28-A/11, Jia Sarai, Near-IIT Hauz Khas, New Delhi-16, Ph : 011-26851008, 26861009