

CSIR-UGC-NET/JRF- DEC - 2014 PHYSICAL SCIENCES BOOKLET - [A]

PART-B

A particle of mass *m* is moving in the potential $V(x) = -\frac{1}{2}ax^2 + \frac{1}{4}bx^4$ where *a*, *b* are positive 21. constants. The frequency of small oscillations about a point of stable equilibrium is (1) $\sqrt{a/m}$ (2) $\sqrt{2a/m}$ (4) $\sqrt{6a/m}$ (3) $\sqrt{3a/m}$ 22. The radius of Earth is approximately 6400 km. The height h at which the acceleration due to Earth's gravity differs from g at the Earth's surface by approximately 1% is (1) 64 km (2) 48 km (3) 32 km (4) 16 km 23. According to the special theory of relativity, the speed v of a free particle of mass m and total energy E is: (1) $v = c_{\sqrt{1 - \frac{mc^2}{E}}}$ (2) $v = \sqrt{\frac{2E}{m}} \left(1 + \frac{mc^2}{E}\right)$ (3) $v = c_{\sqrt{1 - \left(\frac{mc^2}{R}\right)^2}}$ (4) $v = c \left(1 + \frac{mc^2}{E}\right)$ Let \vec{r} denote the position vector of any point in three-dimensional space, and $r = |\vec{r}|$. Then 24. (1) $\vec{\nabla} \cdot \vec{r} = 0$ and $\vec{\nabla} \times \vec{r} = \vec{r} / r$ (2) $\vec{\nabla} \cdot \vec{r} = 0$ and $\nabla^2 r = 0$ (4) $\vec{\nabla} \cdot \vec{r} = 3$ and $\vec{\nabla} \times \vec{r} = 0$ (3) $\vec{\nabla} \cdot \vec{r} = 3$ and $\nabla^2 \vec{r} = \vec{r} / r^2$ The column vector $\begin{pmatrix} a \\ b \\ a \end{pmatrix}$ is a simultaneous eigenvector of $A = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$ and $B = \begin{pmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{pmatrix}$ if 25. (1) b = 0 or a = 0(2) b = a or b = -2a(4) b = a/2 or b = -a/2(3) b = 2a or b = -aCAREER FI The principal value of the integral $\int_{-\infty}^{\infty} \frac{\sin(2x)}{x^3} dx$ is 26. www.careerendeavour.com (2) $-\pi$ (4) 2π (1) -2π Two independent random variables m and n, which can take the integer values 0, 1, 2, \dots, ∞ , 27. follow the Poisson distribution, with distinct mean values μ and v respectively. Then (1) the probability distribution of the random variable l = m + n is a binomial distribution (2) the probability distribution of the random variable r = m - n is also a Poisson distribution (3) the variance of the random variable l = m + n is equal to $\mu + v$ (4) the mean value of the random variable r = m - n is equal to 0. The Laurent series expansion of the function $f(z) = e^{z} + e^{1/z}$ about z = 0 is given by 28. (1) $\sum_{n=\infty}^{\infty} \frac{z^n}{n!}$ for all $|z| < \infty$ (2) $\sum_{n=1}^{\infty} \left(z^n + \frac{1}{z^n} \right) \frac{1}{n!}$ only if 0 < |x| < 1(3) $\sum_{n=1}^{\infty} \left(z^n + \frac{1}{z^n} \right) \frac{1}{n!}$ for all $0 < |z| < \infty$ (4) $\sum_{n=1}^{\infty} \frac{z^n}{n!}$, only if |z| < 1



29. The equation of motion of a system described by the time-dependent Lagrangian $L = e^{\gamma t} \left[\frac{1}{2} m \dot{x}^2 - V(x) \right] \text{ is}$ (1) $m \ddot{x} + \gamma m \dot{x} + \frac{dV}{dx} = 0$ (2) $m \ddot{x} + \gamma m \dot{x} - \frac{dV}{dx} = 0$ (3) $m \ddot{x} - \gamma m \dot{x} + \frac{dV}{dx} = 0$ (4) $m \ddot{x} + \frac{dV}{dx} = 0$

30. A solid sphere of radius *R* has a charge density, given by $\rho(r) = \rho_0 \left(1 - \frac{ar}{R}\right)$, where *r* is the radial coordinate and ρ_0 , *a* and *R* are positive constants. If the magnitude of the electric field at r = R/2

(1) 2 (2) 1 (3)
$$\frac{1}{2}$$
 (4) $\frac{1}{4}$

is 1.25 times that at r = R, then the value of a is

31. The electrostatic lines of force due to a system of four point charges is sketched below.



At a large distance r, the leading asymptotic behaviour of the electrostatic potential is proportional to

- (1) r $(2)/r^{4}$ Careere (3) r^{2} avour (4) r^{4}
- 32. A charged particle moves in a helical path under the influence of a constant magnetic field. The initial velocity is such that the component along the magnetic field is twice the component in the plane normal to the magnetic field. The ratio l/R of the pitch *l* to the radius *R* of the helical path is
 - (1) $\pi/2$ (2) 4π (3) 2π (4) π
- 33. A parallel beam of light of wavelength λ is incident normally on a thin polymer film with air on both sides. If the film has a refractive index n > 1, then second-order bright fringes can be observed in reflection when the thickness of the film is
 - (1) $\lambda/4n$ (2) $\lambda/2n$ (3) $3\lambda/4n$ (4) λ/n



34. Consider the normalized wavefunction $\phi = a_1 \psi_{11} + a_2 \psi_{10} + a_3 \psi_{1-1}$ where ψ_{lm} is a simultaneous normalized eigenfunction of the angular momentum operators L^2 and L_z , with eigenvalues $l(l+1)\hbar^2$ and $m\hbar$ respectively. If ϕ is an eigenfunction of the operator L_x with eigenvalue \hbar , then

(1)
$$a_1 = -a_3 = \frac{1}{2}, a_2 = \frac{1}{\sqrt{2}}$$
 (2) $a_1 = a_3 = \frac{1}{2}, a_2 = \frac{1}{\sqrt{2}}$

(3)
$$a_1 = a_3 = \frac{1}{2}, a_2 = -\frac{1}{\sqrt{2}}$$
 (4) $a_1 = a_2 = a_3 = \frac{1}{\sqrt{3}}$

35. Let x and p denote, respectively, the coordinate and momentum operators satisfying the canonical commutation relation [x, p] = i in natural units $(\hbar = 1)$. Then the commutator $[x, pe^{-p}]$ is

(1)
$$i(1-p)e^{-p}$$
 (2) $i(1-p^2)e^{-p}$ (3) $i(1-e^{-p})$ (4) ipe^{-p}

36. Suppose the Hamiltonian of a conservative system in classical mechanics is $H = \omega x p$, where ω is a constant and x and p are the position and momentum respectively. The corresponding Hamiltonian in quantum mechanics, in the coordinate representation, is

(1)
$$-i\hbar\omega\left(x\frac{\partial}{\partial x}-\frac{1}{2}\right)$$
 (2) $-i\hbar\omega\left(x\frac{\partial}{\partial x}+\frac{1}{2}\right)$ (3) $-i\hbar\omega x\frac{\partial}{\partial x}$ (4) $-\frac{i\hbar\omega}{2}x\frac{\partial}{\partial x}$

Let Ψ_1 and Ψ_2 denote, the normalized eigenstates of a particle with energy eigenvalues E_1 and 37. E_2 respectively, with $E_2 > E_1$. At time t=0 the particle is prepared in a state $\Psi(t=0) = \frac{1}{\sqrt{2}}(\psi_1 + \psi_2)$. The shortest time *T* at which $\Psi(t=T)$ will be orthogonal to $\Psi(t=0)$

is

(1)
$$\frac{2\hbar\pi}{(E_2 - E_1)}$$
 (2) $\frac{\hbar\pi}{(E_2 - E_1)}$ (3) $\frac{\hbar\pi}{2(E_2 - E_1)}$ (4) $\frac{\hbar\pi}{4(E_2 - E_1)}$

38. The I-V characteristics of the diode in the circuit below is given by

$$I = \begin{cases} (V - 0.7) / 500 & \text{for } V \ge 0.7 \\ 0 & \text{for } V < 0.7 \end{cases}$$

where V is measured in volts and I is measured in amperes.

The current I in the circuit is (1) 10.0 mA (2) 9.3 mA

39. A junction is made between a metal of work function W_M , and a doped semiconductor of work function W_s with $W_M > W_s$. If the electric field at the interface has to be increased by a factor of 3, then the dopant concentration in the semiconductor would have to be

10V

(4) 6.7 mA

(3)6.2 mA

- (1) increased by a factor of 9 (2) decreased by a factor of 3
- (3) decreased by a factor of $\sqrt{3}$ (3) increased by a factor of 3

- In a measurement of the viscous drag force experienced by spherical particles in a liquid, the force is found to be proportional to $V^{1/3}$ where V is the measured volume of each particle. If V is measured to be 30 mm³, with an uncertainty of 2.7 mm³, the resulting relative percentage uncertainty in the measured force is
- (1) 2.08 (2) 0.09 (3) 6 (4) 3

41. The pressure *P* of a fluid is related to its number density ρ by the equation of state $P = a\rho + b\rho^2$ where *a* and *b* are constants. If the initial volume of the fluid is V_0 , the work done on the system when it is compressed so as to increase the number density from an initial value of ρ_0 to $2\rho_0$ is

(1)
$$a\rho_0 V_0$$
 (2) $(a+b\rho_0)\rho_0 V_0$

(3)
$$\left(\frac{3a}{2} + \frac{7\rho_0 b}{3}\right)\rho_0 V_0$$
 (4) $(a\ln 2 + b\rho_0)\rho_0 V_0$

42. The Hamiltonian of a classical particle moving in one dimension is $H = \frac{p^2}{2m} + \alpha q^4$ where α is a positive constant and p and q are its momentum and position respectively. Given that its total energy $E \le E_0$ the available volume of phase space depends on E_0 as

(1)
$$E_0^{3/4}$$
 (2) E_0 (3) $\sqrt{E_0}$ (4) is independent of E_0

43. An ideal Bose gas is confined inside a container that is connected to a particle reservoir. Each particle can occupy a discrete set of single-particle quantum states. If the probability that a particular quantum state is unoccupied is 0.1, then the average number of bosons in that state is (1) 8 (2) 9 (3) 10 (4) 11

44. In low density oxygen gas at low temperature, only the translational and rotational modes of the molecules are excited. The specific heat per molecule of the gas is

(1)
$$\frac{1}{2}k_B$$
 (2) k_B (3) $\frac{3}{2}k_B$ (4) $\frac{5}{2}k_B$

45. Consider the amplifier circuit comprising of the two op-amps A_1 and A_2 as shown in the figure If the input ac signal source has an impedance of $50k\Omega$, which of the following statements is true?



- (1) A_1 is required in the circuit because the source impedance is much greater than r
- (2) A_1 is required in the circuit because the source impedance is much less than R
- (3) A_1 can be eliminated from the circuit without affecting the overall gain
- (4) A_1 is required in the circuit if the output has to follow the phase of the input signal

40.



PART-C

- 46. A plane electromagnetic wave incident normally on the surface of a material is partially reflected. Measurements on the standing wave in the region in front of the interface show that the ratio of the electric field amplitude at the maxima and the minima is 5. The ratio of the reflected intensity to the incident intensity is

 (1) 4/9
 (2) 2/3
 (3) 2/5
 (4) 1/5
- 47. The scalar and vector potentials $\varphi(\vec{x},t)$ and $\vec{A}(\vec{x},t)$ are determined up to a gauge transformation

$$\phi \to \phi' = \phi - \frac{\partial \xi}{\partial t}$$
 and $\vec{A} \to \vec{A}' = \vec{A} + \vec{\nabla} \xi$ where ξ is an arbitrary continuous and differentiable

function of \vec{x} and *t*. If we further impose the Lorenz gauge condition $\vec{\nabla} \cdot \vec{A} + \frac{1}{c} \frac{\partial \varphi}{\partial t} = 0$ then a

possible choice for the gauge function $\xi(\vec{x},t)$ is (where ω, \vec{k} are nonzero constants with $\omega = c |\vec{k}|$)

- (1) $\cos \omega t \cosh \vec{k} \cdot \vec{x}$ (2) $\sinh \omega t \cos \vec{k} \cdot \vec{x}$
- (3) $\cosh \omega t \cos \vec{k} \cdot \vec{x}$ (4) $\cosh \omega t \cosh \vec{k} \cdot \vec{x}$
- 48. A non-relativistic particle of mass *m* and charge *e*, moving with a velocity \vec{v} and acceleration \vec{a} , emits radiation of intensity *I*. What is the intensity of the radiation emitted by a particle of mass m/2, charge 2*e*, velocity $\vec{v}/2$ and acceleration $2\vec{a}$? (1) 16 *I* (2) 8 *I* (3)4 *I* (4) 2 *I*
- 49. Let α and β be complex numbers. Which of the following sets of matrices forms a group under matrix multiplication?

(1)
$$\begin{pmatrix} \alpha & \beta \\ 0 & 0 \end{pmatrix}$$
 (2) $\begin{pmatrix} 1 & \alpha \\ \beta & 1 \end{pmatrix}$, where $\alpha\beta \neq 1$

(3)
$$\begin{pmatrix} \alpha & \alpha^* \\ \beta & \beta^* \end{pmatrix}$$
, where $\alpha \beta^*$ is

(4)
$$\begin{pmatrix} \alpha & \beta \\ -\beta^* & \alpha^* \end{pmatrix}$$
, where $|\alpha|^2 + |\beta|^2 =$

1

50. The expression $\sum_{i,j,k=1}^{3} \in_{ijk} \{x_i, \{p_j, L_k\}\}$ (where \in_{ijk} is the Levi-Civita symbol, $\vec{x}, \vec{p}, \vec{L}$ are the position, momentum and angular momentum respectively, and $\{A, B\}$ represents the Poisson bracket of A and B) simplifies to

(1) 0 (2) 6 (3) $\vec{x} \cdot (\vec{p} \times \vec{L})$ (4) $\vec{x} \times \vec{p}$

51. A mechanical system is described by the Hamiltonian $H(q, p) = \frac{p^2}{2m} + \frac{1}{2}m\omega^2 q^2$. As a result of the

canonical transformation generated by $F(q,Q) = -\frac{Q}{q}$, the Hamiltonian in the new coordinate Q and momentum P becomes

(1) $\frac{1}{2m}Q^2P^2 + \frac{m\omega^2}{2}Q^2$ (2) $\frac{1}{2m}Q^2P^2 + \frac{m\omega^2}{2}P^2$ (3) $\frac{1}{2m}P^2 + \frac{m\omega^2}{2}Q^2$ (4) $\frac{1}{2m}Q^2P^4 + \frac{m\omega^2}{2}P^{-2}$



- 52. Let $\vec{\sigma} = (\sigma_1, \sigma_2, \sigma_3)$, where $\sigma_1, \sigma_2, \sigma_3$ are the Pauli matrices. If \vec{a} and \vec{b} are two arbitrary constant vectors in three dimensions, the commutator $[\vec{a} \cdot \vec{\sigma}, \vec{b} \cdot \vec{\sigma}]$ is equal to (in the following *I* is the identity matrix)
 - (1) $(\vec{a} \cdot \vec{b})(\sigma_1 + \sigma_2 + \sigma_3)$ (2) $2i(\vec{a} \times \vec{b}) \cdot \vec{\sigma}$

(3)
$$(\vec{a} \cdot \vec{b})I$$
 (4) $|\vec{a}||\vec{b}|I$

53. Consider the function $f(z) = \frac{1}{z} \ln(1-z)$ of a complex variable $z = re^{i\theta} (r \ge 0, -\infty < \theta < \infty)$. The singularities of f(z) are as follows:

- (1) branch points at z=1 and $z=\infty$; and a pole at z=0 only for $0 \le \theta < 2\pi$
- (2) branch points at z=1 and $z=\infty$; and a pole at z=0 for all θ other than $0 \le \theta < 2\pi$
- (3) branch points at z=1 and $z=\infty$; and a pole at z=0 for all θ
- (4) branch points at z=0, z=1 and $z=\infty$

54. The function
$$f(x) = \sum_{n=0}^{\infty} \frac{(-1)^n}{n!(n+1)!} \left(\frac{x}{2}\right)^{2n+1}$$
 satisfies the differential equation
(1) $x^2 \frac{d^2 f}{dx^2} + x \frac{df}{dx} + (x^2+1)f = 0$ (2) $x^2 \frac{d^2 f}{dx^2} + 2x \frac{df}{dx} + (x^2-1)f = 0$
 $d^2 f = df$

(3)
$$x^2 \frac{d^2 f}{dx^2} + x \frac{df}{dx} + (x^2 - 1)f = 0$$
 (4) $x^2 \frac{d^2 f}{dx^2} - x \frac{df}{dx} + (x^2 - 1)f = 0$

55. The probe *Mangalyaan* was sent recently to explore the planet Mars. The inter-planetary parts of the trajectory is approximately a half-ellipse with the Earth (at the time of launch), Sun and Mars (at the time the probe reaches the destination) forming the major axis. Assuming that the orbits of Earth and Mars are approximately circular with radii R_E and R_M , respectively, the velocity (with respect to the Sun) of the probe during its voyage when it is at a distance $r(R_E \ll r \ll R_M)$ from the Sun, neglecting the effect of Earth and Mars, is

(1)
$$\sqrt{2GM \frac{(R_E + R_M)}{r(R_E + R_M - r)}}$$
 (2) $\sqrt{2GM \frac{(R_E + R_M - r)}{r(R_E + R_M)}}$
(3) $\sqrt{2GM \frac{R_E}{rR_M}}$ (4) $\sqrt{\frac{2GM}{r}}$

- 56. A large MOS transistor consists of N individual transistors connected in parallel. If the only form of noise in each transistor is 1/f noise, then the equivalent voltage noise spectral density for the MOS transistor is
 - (1) 1/N times that of a single transistor
- (2) $1/N^2$ times that of a single transistor
- (3) N times that of a single transistor
- (4) N^2 times that of a single transistor



57. Consider a particle of mass *m* in the potential V(x) = a |x|, a > 0. The energy eigen-values $E_n (n = 0, 1, 2, ...)$, in the WKB approximation, are

(1)
$$\left[\frac{3a\hbar\pi}{4\sqrt{2m}}\left(n+\frac{1}{2}\right)\right]^{1/3}$$
 (2) $\left[\frac{3a\hbar\pi}{4\sqrt{2m}}\left(n+\frac{1}{2}\right)\right]^{2/3}$ (3) $\frac{3a\hbar\pi}{4\sqrt{2m}}\left(n+\frac{1}{2}\right)$ (4) $\left[\frac{3a\hbar\pi}{4\sqrt{2m}}\left(n+\frac{1}{2}\right)\right]^{4/3}$

- 58. When laser light of wavelength λ falls on a metal scale with 1mm engravings at a grazing angle of incidence, it is diffracted to form a vertical chain of diffraction spots on a screen kept perpendicular to the scale. if the wavelength of the laser is increased by 200nm, the angle of the first-order diffraction spot changes from 5° to
 - (1) 6.60° (2) 5.14° (3) 5.018° (4) 5.21°

59. Let $|\psi\rangle = c_0 |0\rangle + c_1 |1\rangle$ (where c_0 and c_1 are constants with $c_0^2 + c_1^2 = 1$) be a linear combination of the wavefunctions of the ground and first excited states of the one-dimensional harmonic oscillator. For what value of c_0 is the expectation value $\langle x \rangle$ a maximum?

(1)
$$\langle x \rangle = \sqrt{\frac{\hbar}{m\omega}}, c_0 = \frac{1}{\sqrt{2}}$$

(2) $\langle x \rangle = \sqrt{\frac{\hbar}{2m\omega}}, c_0 = \frac{1}{2}$
(3) $\langle x \rangle = \sqrt{\frac{\hbar}{2m\omega}}, c_0 = \frac{1}{\sqrt{2}}$
(4) $\langle x \rangle = \sqrt{\frac{\hbar}{m\omega}}, c_0 = \frac{1}{2}$

60. Consider a Low Pass (LP) and a High Pass (HP) filter with cut-off frequencies f_{LP} and f_{HP} , respectively, connected in series or in parallel configurations as shown in the Figures A and B below.



Which of the following statements is correct?

(1) For $f_{HP} < f_{LP}$, A acts as a Band Pass filter and B acts as a Band Reject filter

(2) For $f_{HP} > f_{LP}$, A stops the signal from passing through and B passes the signal without filtering

- (3) For $f_{HP} < f_{LP}$, A acts as a Band Pass filter and B passes the signal without filtering
- (4) For $f_{HP} > f_{LP}$, A passes the signal without filtering and B acts as a Band Reject filter



61. A collection N of non-interacting spins S_i , i = 1, 2, ..., N, $(S_i = \pm 1)$ is kept in an external magnetic field B at a temperature T. The Hamiltonian of the system is $H = -\mu B \sum_{i} S_{i}$. What should be the

minimum value of
$$\frac{\mu B}{k_B T}$$
 for which the mean value $\langle S_i \rangle \ge \frac{1}{3}$?

- (3) $\frac{1}{2} \ln 2$ (4) $N \ln 2$ (1) $\frac{1}{2}N\ln 2$ (2) $2\ln 2$
- When a gas expands adiabatically from volume V_1 to V_2 by a quasi-static reversible process, it cools from temperature T_1 to T_2 . If now the same process is carried out adiabatically and irreversibly, 62. and T'_2 is the temperature of the gas when it has equilibrated, then

(1)
$$T'_{2} = T_{2}$$
 (2) $T'_{2} > T_{2}$ (3) $T'_{2} = T_{2} \left(\frac{V_{2} - V_{1}}{V_{2}} \right)$ (4) $T'_{2} = \frac{T_{2}V_{1}}{V_{2}}$

63. A random walker takes a step of unit length in the positive direction with probability 2/3 and a step of unit length in the negative direction with probability 1/3. The mean displacement of the walker after n steps is (2) n/8(3) 2n/3(4) 0

- The Hamiltonian H_0 for a three-state quantum system is given by the matrix $H_0 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{pmatrix}$. 64.

When perturbed by $H' = \in \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$ where $\in \ll 1$, the resulting shift in the energy eigenvalue

- $E_0 = 2$ is (2) −∈,2∈ (1) ∈,−2∈ (3) ± ∈ (4) ±2 ∈
- The ground state energy of the attractive delta function potential $V(x) = -b\delta(x)$, where b > 0, 65.

calculated with the variational trial function $\psi(x) = \begin{cases} A \cos \frac{\pi x}{2a}, & \text{for} - a < x < a, \\ 0, & \text{otherwise,} \end{cases}$ is

(1)
$$-\frac{mb^2}{\pi^2\hbar^2}$$
 (2) $-\frac{2mb^2}{\pi^2\hbar^2}$ (3) $-\frac{mb^2}{2\pi^2\hbar^2}$ (4) $-\frac{mb^2}{4\pi^2\hbar^2}$

66. If the binding energy B of a nucleus (mass number A and charge Z) is given by

$$B = a_V A - a_S A^{2/3} - a_{sym} \frac{(2Z - A)^2}{A} - \frac{a_c Z^2}{A^{1/3}}$$
 where $a_V = 16$ MeV, $a_S = 16$ MeV, $a_{sym} = 24$ MeV and $a_c = 0.75$ MeV, then the Z for the most stable isobar for a nucleus with $A = 216$ is
(1) 68 (2) 72 (3) 84 (4) 92



67. Consider the crystal structure of sodium chloride which is modeled as a set of touching spheres. Each sodium atom has a radius r_1 and each chlorine atom has a radius r_2 . The centres of the spheres form a simple cubic lattice. The packing fraction of this system is

(1)
$$\pi \left[\left(\frac{r_1}{r_1 + r_2} \right)^3 + \left(\frac{r_2}{r_1 + r_2} \right)^3 \right]$$

(2) $\frac{2\pi}{3} \frac{r_1^3 + r_2^3}{(r_1 + r_2)^3}$
(3) $\frac{r_1^3 + r_2^3}{(r_1 + r_2)^3}$
(4) $\pi \frac{r_1^3 + r_2^3}{2(r_1 + r_2)^3}$

- 68. Consider two crystalline solids, one of which has a simple cubic structure, and the other has a tetragonal structure. The effective spring constant between atoms in the *c*-direction is half the effective spring constant between atoms in the *a* and *b* directions. At low temperatures, the behaviour of the lattice contribution to the specific heat will depend as a function of temperature T as
 - (1) T^2 for the tetragonal solid, but as T^3 for the simple cubic solid
 - (2) T for the tetragonal solid and as T^3 for the simple cubic solid
 - (3) T for both solids
 - (4) T^3 for both solids
- 69. An atomic transition ${}^{1}P \rightarrow {}^{1}S$ in a magnetic field 1 Tesla shows Zeeman splitting. Given that the Bohr magneton $\mu_{B} = 9.27 \times 10^{-24}$ J/T, and the wavelength corresponding to the transition is 250 nm, the separation in the Zeeman spectral lines is approximately (1) 0.01 nm (2) 0.1 nm (3) 1.0 nm (4) 10 nm
- 70. If the leading anharmonic correction to the energy of the *n*-th vibrational level of a diatomic molecule is $-x_e \left(n + \frac{1}{2}\right)^2 \hbar \omega$ with $x_e = 0.001$, the total number of energy levels possible is approximately (1) 500 (2) 1000 (3) 250 (4) 750
- 71. A superconducting ring carries a steady current in the presence of a magnetic field \vec{B} normal to the plane of the ring. Identify the *incorrect* statement.
 - (1) The flux passing through the superconductor is quantized in units of hc/e
 - (2) The current and the magnetic field in the superconductor are time independent

(3) The current density \vec{J} and \vec{B} are related by the equation $\vec{\nabla} \times \vec{J} + \Lambda^2 \vec{B} = 0$, where Λ is a constant

(4) The superconductor shows an energy gap which is proportional to the transition temperature of the superconductor



72. The effective spin-spin interaction between the electron spin \vec{s}_e and the proton spin \vec{s}_p in the ground state of the Hydrogen atom is given by $H' = a\vec{s}_e \cdot \vec{s}_p$. As a result of this interaction, the energy levels split by an amount

(1)
$$\frac{1}{2}a\hbar^2$$
 (2) $2a\hbar^2$ (3) $a\hbar^2$ (4) $\frac{3}{2}a\hbar^2$

73. In deep inelastic scattering electrons are scattered off protons to determine if a proton has any internal structure. The energy of the electron for this must be at least (1) 1.25×10^9 eV (2) 1.25×10^{12} eV (3) 1.25×10^6 eV (4) 1.25×10^8 eV

74. The power density of sunlight incident on a solar cell is 100 mW/cm². Its short circuit current density is 30 mA/cm² and the open circuit voltage is 0.7 V. If the fill factor of the solar cell decreases from 0.8 to 0.5 then the percentage efficiency will decrease from

(1) 42.0 to 26.2 (2) 24.0 to 16.8 (4) 16.8 to 10.5 (3) 21.0 to 10.5 75. Consider the four processes (ii) $\Lambda^0 \rightarrow p^+ + e^+ + v_e$ (i) $p^+ \rightarrow n + e^+ + v_a$ (iii) $\pi^+ \rightarrow e^+ + v_e$ (iv) $\pi^0 \rightarrow \gamma + \gamma$ Which of the above is/are forbidden for free particles? (1) only (ii) (2) (ii) and (iv) (4) (i) and (ii) (3)(i) and (iv)CAREER ENDEAVOUR