PHYSICS-PH

Q.1 – Q.30 : Carry ONE mark each.

- 1. The average value of the function $f(x) = 4x^3$ in the interval 1 to 3 is (a) 15 (b) 20 (c) 40 (d) 80
- 2. The unit normal to the curve $x^3 y^2 + xy = 17$ at the point (2, 0) is

(a)
$$\frac{(\hat{i} + \hat{j})}{\sqrt{2}}$$
 (b) $-\hat{i}$ (c) $-\hat{j}$ (d) \hat{j}

3. The value of the integral $\int_C \frac{dz}{z+3}$, where C is a circle (anticlockwise) with |z| = 4, is

(a) 0 (b)
$$\pi i$$
 (c) $2\pi i$ (d) $4\pi i$

4. The determinant of a 3×3 real symmetric matrix is 36. If two of its eigen values are 2 and 3 then the third eigenvalue is

- (a) 4 (b) 6 (c) 8 (d) 9
- 5. For a particle moving in a central field
 (a) the kinetic energy is a constant of motion
 (b) the potential energy is velocity dependent
 (c) the motion is confined in a plane
 (d) the total energy is not conserved
- 6. A bead of mass *m* slides along a straight frictionless rigid wire rotating in a horizontal plane with a constant angular speed ω . The axis of rotation is perpendicular to the wire and passes through one end of the wire. If *r* is the distance of the mass from the axis of rotation and *v* is its speed then the magnitude of the Coriolis force is

(a)
$$\frac{mv^2}{r}$$
 (b) $\frac{2mv}{r}$

7. If for a system of *N* particles of different masses $m_1, m_2, ..., m_N$ with position vectors $\vec{r_1}, \vec{r_2}, ..., \vec{r_N}$ and

(c) $mv\omega$

(d) $2mv\omega$

corresponding velocities $\vec{v}_1, \vec{v}_2, ..., \vec{v}_N$, respectively, such that $\sum \vec{v}_i = 0$, then

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- (a) the total momentum MUST be zero ERE
- (b) the total angular momentum MUST be independent of the choice of the origin
- (c) the total force on the system MUST be zero
- (d) the total torque on the system MUST be zero
- 8. Although mass-energy equivalence of special relativity allows conversion of a photon to an electron-positron pair, such a process cannot occur in free space because
 - (a) the mass is not conserved (b) the energy is not conserved
 - (c) the momentum is not conserved (d) the charge is not conserved
- 9. Three infinitely long wires are placed equally apart on the circumference of a circle of radius *a*, perpendicular to its plane. Two of the wires carry current *I* each, in the same direction, while the third carries current 2*I* along the direction opposite to the other two. The magnitude of the magnetic induction \vec{B} at a distance r from the centre of the circle, for r > a, is

(a) 0 (b)
$$\frac{2\mu_0}{\pi} \frac{I}{r}$$
 (c) $-\frac{2\mu_0}{\pi} \frac{I}{r}$ (d) $\frac{2\mu_0}{\pi} \frac{Ia}{r^2}$



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QUESTION PAPER

10. A solid sphere of radius R carries a uniform volume charge density ρ . The magnitude of electric field inside the sphere at a distance *r* from the centre is

(a)
$$\frac{r\rho}{3\varepsilon_0}$$
 (b) $\frac{R\rho}{2\varepsilon_0}$ (c) $\frac{R^2\rho}{r\varepsilon_0}$ (d) $\frac{R^3\rho}{r^2\varepsilon_0}$

- The electric field $\vec{E}(\vec{r}, t)$ for a circularly polarized electromagnetic wave propagating along the position z-11. direction is
 - (a) $E_0(\hat{x} + \hat{y}) \exp[i(kz \omega t)]$ (b) $E_0(\hat{x}+i\hat{y}) \exp[i(kz-\omega t)]$ (c) $E_0(\hat{x}+i\hat{y})\exp[i(kz+\omega t)]$ (d) $E_0(\hat{x} + \hat{y}) \exp[i(kz + \omega t)]$
- 12. The electric (E) and magnetic (B) field amplitudes associated with an electromagnetic radiation from a point source behave at a distance r from the source as
 - (b) $E \propto \frac{1}{r}, B \propto \frac{1}{r}$ (a) E = constant, B = constant1 1 (d) $E \propto \frac{1}{r^3}, B \propto \frac{1}{r^3}$

(c)
$$E \propto \frac{1}{r^2}, B \propto \frac{1}{r^2}$$

- The parities of the wave functions 13.
 - (i) $\cos(kx)$, and
 - (ii) and $\tan h(kx)$ are
 - (b) (i) even, (ii) even (c) (i) odd, (ii) even (a) (i) odd, (ii) odd (d) (i) even, (ii) odd
- The commutator, $[L_z, Y_{lm}(\theta, \phi)]$, where L_z is the z-component of the orbital angular momentum and $Y_{lm}(\theta, \phi)$ 14. is a spherical harmonic, is
 - (a) $l(l+1)\hbar Y_{lm}(\theta,\phi)$ (b) $-m\hbar Y_{lm}(\theta,\phi)$ (c) $m\hbar Y_{lm}(\theta,\phi)$ (d) $+l\hbar Y_{lm}(\theta,\phi)$
- A system in a normalized state $|\psi\rangle = c_1 |\alpha_1\rangle + c_2 |\alpha_2\rangle$, with $|\alpha_1\rangle$ and $|\alpha_2\rangle$ representing two different 15. eigenstates of the system, requires that the constants c_1 and c_2 must satisfy the condition

(a)
$$|c_1| \cdot |c_2| = 1$$
 (b) $|c_1| + |c_2| = 1$ (c) $(|c_1| + |c_2|)^2 = 1$ (d) $|c_1|^2 + |c_2|^2 = 1$

A one dimensional harmonic oscillator carrying a charge -q is placed in a uniform electric field \vec{E} along the 16. positive x-axis. The corresponding Hamiltonian operator is

(a)
$$\frac{\hbar^2}{2m} \frac{d^2}{dx^2} + \frac{1}{2}kx^2 + qEx$$

(b) $\frac{\hbar^2}{2m} \frac{d^2}{dx^2} + \frac{1}{2}kx^2 - qEx$
(c) $-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} + \frac{1}{2}kx^2 + qEx$
(d) $-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} + \frac{1}{2}kx^2 - qEx$

- The L_{β} line of X-rays emitted from an atom with principal quantum numbers n = 1, 2, 3, ..., arises from the 17. transition
 - (c) $n = 5 \rightarrow n = 2$ (d) $n = 3 \rightarrow n = 1$ (a) $n = 4 \rightarrow n = 2$ (b) $n = 3 \rightarrow n = 2$
- For an electron in hydrogen atom, the states are characterized by the usual quantum numbers n, l, m_l . The 18. electric dipole transition between any two states requires that
 - (a) $\Delta l = 0, \ \Delta m_l = 0, \pm 1$ (b) $\Delta l = \pm 1, \ \Delta m_l = \pm 1, \pm 2$
 - (d) $\Delta l = \pm 1, \ \Delta m_l = 0, \pm 2$ (c) $\Delta l = \pm 1, \ \Delta m_l = 0, \pm 1$



- 19. If the equation of state for a gas with internal energy U is $pV = \frac{1}{3}U$, then the equation for an adiabatic process is
 - (a) $pV^{1/3} = \text{constant}$ (b) $pV^{2/3} = \text{constant}$ (c) $pV^{4/3} = \text{constant}$ (d) $pV^{3/5} = \text{constant}$
- 20. The total number of accessible states of N non-interacting particles of spin $-\frac{1}{2}$ is

(a)
$$2^N$$
 (b) N^2 (c) $2^{N/2}$ (d) N

21. The pressure for a non-interacting Fermi gas with internal energy U at temperature T is

(a)
$$p = \frac{3}{2} \frac{U}{V}$$
 (b) $p = \frac{2}{3} \frac{U}{V}$ (c) $p = \frac{3}{5} \frac{U}{V}$ (d) $p = \frac{1}{2} \frac{U}{V}$

22. A system of non-interacting Fermi particles with Fermi energy E_F has the density of states proportional to \sqrt{E} , where *E* is the energy of a particle. The average energy per particle at temperature T = 0 is $1 - \frac{1}{2} - \frac{2}{3} - \frac{3}{3} - \frac$

(a)
$$\frac{1}{6}E_F$$
 (b) $\frac{1}{5}E_F$ (c) $\frac{2}{5}E_F$ (d) $\frac{3}{5}E_F$

23. In crystallographic notations the vector \overline{OP} in the cubic cell shown in the figure is



25. The evidence for the non-conservation of parity in β - decay has been obtained from the observation that the

 β intensity

- (a) antiparallel to the nuclear spin directions is same as that along the nuclear spin direction
- (b) antiparallel to the nuclear spin direction is not the same as that along the nuclear spin direction
- (c) shows a continuous distribution as a function of momentum
- (d) is independent of the nuclear spin direction



26. Which of the following expressions for total binding energy *B* of a nucleus is correct $(a_1, a_2, a_3, a_4 > 0)$?

(b)
$$B = a_1 A - a_2 A^{2/3} - a_3 \frac{Z(Z-1)}{A^{1/3}} - a_4 \frac{(A-2Z)^2}{A} + \delta$$

(b)
$$B = a_1 A + a_2 A^{2/3} - a_3 \frac{Z(Z-1)}{A^{1/3}} - a_4 \frac{(A-2Z)^2}{A} + \delta$$

(c)
$$B = a_1 A + a_2 A^{1/3} - a_3 \frac{Z(Z-1)}{A^{1/3}} - a_4 \frac{(A-2Z)^2}{A} + \delta$$

(d)
$$B = a_1 A - a_2 A^{1/3} - a_3 \frac{Z(Z-1)}{A^{1/3}} - a_4 \frac{(A-2Z)^2}{A} + \delta$$

- 27. Which of the following decay is forbidden ?
 - (a) $\mu^- \rightarrow e^- + v_\mu + \overline{v}_c$ (b) $\pi^+ \rightarrow \mu^+ + v_\mu$ (c) $\pi^+ \rightarrow e^+ + v_e$ (d) $\mu^- \rightarrow e^+ + e^- + e^-$
- 28. With reference to nuclear forces which of the following statements is NOT true ? The nuclear forces are
 (a) short range
 (b) charge independent (c) velocity dependent (d) spin independent

(b) voltage controlled voltage source

- 29. A junction field effect transistor behaves as a
 - (a) voltage controlled current source
 - (c) current controlled voltage source (d) current controlled current source
- 30. The circuit shown can be used as $V_{in1} \rightarrow V_{out}$ $V_{in2} \rightarrow V_{out}$ (a) NOR gate (b) OR gate (c) NAND gate (d) AND gate

Q.31 – Q.80 : Carry TWO marks each.

31. If a vector field
$$\vec{F} = x\hat{i} + 2y\hat{j} + 3z\hat{k}$$
, then $\vec{\nabla} \times (\vec{\nabla} \times \vec{F})$ is
(a) 0 (b) \hat{i} (c) $2\hat{j}$ (d) $3\hat{k}$

- 32. All solutions of the equation $e^z = -3$ are
 - (a) $z = in \pi \ln 3, n = \pm 1, \pm 2, ...$ (b) $z = \ln 3 + i(2n+1)\pi, n = 0, \pm 1, \pm 2, ...$ (c) $z = \ln 3 + i 2n\pi, n = 0, \pm 1 \pm 2, ...$ (d) $z = i 3n\pi, n = \pm 1 \pm 2, ...$
- 33. If $\overline{f}(s)$ is the Laplace transform of f(t) the Laplace transform of f(at), where a is a constant, is

(a)
$$\frac{1}{a}\overline{f}(s)$$
 (b) $\frac{1}{a}\overline{f}(s/a)$ (c) $\overline{f}(s)$ (d) $\overline{f}(s/a)$



34.	Given the four vectors	
	$u_1 = \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix}, u_2 = \begin{pmatrix} 3 \\ -5 \\ 1 \end{pmatrix}, u_3 = \begin{pmatrix} 2 \\ 4 \\ -8 \end{pmatrix}, u_4 = \begin{pmatrix} 2 \\ 4 \\ -8 \end{pmatrix}, u_5 =$	$u_4 = \begin{pmatrix} 3\\ 6\\ -12 \end{pmatrix}$
	the linearly dependent pair is	
	(a) $u_1 u_2$ (b) $u_1 u_3$	(c) $u_1 u_4$ (d) $u_3 u_4$
35.	Consider the following function: $f(z) = \frac{\sin z}{z}$. Which of the following statemens is are TRUE?
	(a) $z = 0$ is pole of order 1 (c) $z = 0$ is a pole order 3	(b) $z = 0$ is a removable singular point (d) $z = 0$ is an essential singular point
36.	Eigen values of the matrix	
	$\begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -2i \\ 0 & 0 & 2i & 0 \end{pmatrix}$ are	e
	(a) $-2, -1, 1, 2$ (b) $-1, 1, 0, 2$	(c) 1, 0, 2, 3 (d) -1, 1, 0, 3
37. If a particle moves outward in a plane ald are constants, then its		curved trajectory described by $r = a\theta$, $\theta = \omega t$, where a and ω
	(a) Kinetic energy is conserved (c) total momentum is conserved	(b) angular momentum is conserved (d) radial momentum is conserved
38.	A circular hoop of mass M and radius a rolls wi	thout slipping with constant angular speed ω along the horizon-
	tal x-axis in the xy-plane. When the centre of the hoop is at a distance $d = \sqrt{2}a$ from the origin, the magnitude	

tal *x*-axis in the *xy*-plane. When the centre of the hoop is at a distance $d = \sqrt{2a}$ from the origin, the magnitude of the total angular momentum of the hoop about the origin is

(a)
$$Ma^2\omega$$
 (b) $\sqrt{2}Ma^2\omega$ (c) $2Ma^2\omega$ (d) $3Ma^2\omega$

39. Two solid spheres of radius R and mass M each are connected by a thin rigid rod of negligible mass. The distance between the centres is 4R. The moment of inertia about an axis passing through the centre of symmetry and perpendicular to the line joining the spheres is

(a)
$$\frac{11}{5}MR^2$$
 (b) $\frac{22}{5}MR^2$ (c) $\frac{44}{5}MR^2$ (d) $\frac{88}{5}MR^2$

40. A car is moving with constant linear acceleration a along horizontal x-axis. A solid sphere of mass M and radius R is found rolling without slipping on the horizontal floor of the car in the same direction as seen from an inertial frame outside the car. The acceleration of the sphere in the inertial frame is

(a)
$$\frac{a}{7}$$
 (b) $\frac{2a}{7}$ (c) $\frac{3a}{7}$ (d) $\frac{5a}{7}$

41. A rod of length l_0 makes an angle θ_0 with the y-axis in its rest frame, while the rest frame moves to the right

along the *x*-axis with relativistic speed *v* with respect to the lab frame. If $\gamma = \left(1 - \frac{v^2}{c^2}\right)^{-1/2}$, the angle θ in the

lab frame is

(a)
$$\theta = \tan^{-1}(\gamma \tan \theta_0)$$

(b) $\theta = \tan^{-1}(\gamma \cot \theta_0)$
(c) $\theta = \tan^{-1}\left(\frac{1}{\gamma} \tan \theta_0\right)$
(d) $\theta = \tan^{-1}\left(\frac{1}{\gamma} \cot \theta_0\right)$



QUESTION PAPER

- 42. A particle of mass *m* moves in a potential $V(x) = \frac{1}{2}m\omega^2 x^2 + \frac{1}{2}m\mu v^2$, where *x* is the position coordinate, *v* is the speed, and ω and μ are constants. The canonical (conjugate) momentum of the particle is (a) $p = m(1+\mu)v$ (b) p = mv (c) $p = m\mu v$ (d) $p = m(1-\mu)v$
- 43. Consider the following three independent cases :
 - (i) Particle A of charge +q moves in free space with a constant velocity \vec{v} ($v \ll$ speed of light)
 - (ii) Particle B of charge +q moves in free space in a circle of radius R with same speed v as in case (i)
 - (iii) Particle C having charge -q moves as in case (ii)

If the power radiated by A, B and C are P_A , P_B and P_C , respectively, then

- (a) $P_A = 0, P_B > P_C$ (b) $P_A = 0, P_B = P_C$ (c) $P_A > P_B > P_C$ (d) $P_A = P_B = P_C$
- 44. If the electrostatic potential were given by $\phi = \phi_0 (x^2 + y^2 + z^2)$, where ϕ_0 is constant, then the charge density giving rise to the above potential would be

(a) 0 (b)
$$-6\phi_0\varepsilon_0$$
 (c) $-2\phi_0\varepsilon_0$ (d) $-\frac{6\phi_0}{\varepsilon_0}$

45. The work done in bringing a charge +q from infinity in free space, to a position at a distance d in front of a semi-infinite grounded metal surface is

(a)
$$-\frac{q^2}{4\pi\varepsilon_0(d)}$$
 (b) $-\frac{q^2}{4\pi\varepsilon_0(2d)}$ (c) $-\frac{q^2}{4\pi\varepsilon_0(4d)}$ (d) $-\frac{q^2}{4\pi\varepsilon_0(6d)}$

46. A plane electromagnetic wave travelling in vacuum is incident normally on a non-magnetic, non-absorbing medium of refractive index *n*. The incident (E_i) , reflected (E_r) and transmitted (E_t) electric fields are given as, $E_i = E \exp[i(k_z - \omega t)]$, $E_r = E_{0r} \exp[i(k_r z - \omega t)]$, $E_t = E_{0t} \exp[i(k_t z - \omega t)]$. If E = 2 V/m and

n = 1.5, then the application of appropriate boundary conditions leads to

- (a) $E_{0r} = -\frac{3}{5}$ V/m, $E_{0t} = \frac{7}{5}$ V/m (b) $E_{0r} = -\frac{1}{5}$ V/m, $E_{0t} = \frac{8}{5}$ V/m (c) $E_{0r} = -\frac{2}{5}$ V/m, $E_{0t} = \frac{8}{5}$ V/m (d) $E_{0r} = \frac{4}{5}$ V/m, $E_{0t} = \frac{6}{5}$ V/m
- 47. For a vector potential \vec{A} , the divergence of \vec{A} is $\vec{\nabla} \cdot \vec{A} = -\frac{\mu_0}{4\pi} \frac{Q}{r^2}$, where Q is a constant of appropriate

dimension. The corresponding scalar potential $\varphi(\vec{r}, t)$ that makes \vec{A} and φ Lorentz gauge invariant is

(a)
$$\frac{1}{4\pi\varepsilon_0} \frac{Q}{r}$$
 (b) $\frac{1}{4\pi\varepsilon_0} \frac{Qt}{r}$ (c) $\frac{1}{4\pi\varepsilon_0} \frac{Q}{r^2}$ (d) $\frac{1}{4\pi\varepsilon_0} \frac{Qt}{r^2}$

48. An infinitely long wire carrying a current $I(t) = I_0 \cos(\omega t)$ is placed at a distance *a* from a square loop of side *a* as shown in the figure. If the resistance of the loop is *R*, then the amplitude of the induced current in the loop is



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QUESTION PAPER

- 59. The typical wavelengths emitted by diatomic molecules in purely vibrational and purely rotational transitions are respectively in the region of
 - (a) infrared and visible
 - (c) infrared and microwave
- (b) visible and infrared
- (d) microwave and infrared

60. In a two electron atomic system having orbital and spin angular momenta l_1 , l_2 and s_1 , s_2 respectively, the coupling strengths are defined as $\Gamma_{l_1 l_2}$, $\Gamma_{s_1 s_2}$, $\Gamma_{l_1 s_1}$, $\Gamma_{l_2 s_2}$, $\Gamma_{l_1 s_2}$ and $\Gamma_{l_2 s_1}$. For the *jj* coupling scheme to be applicable, the coupling strengths MUST satisfy the condition

61. If the probability that x lies between x and x + dx is $p(x)dx = ae^{-ax}dx$, where $0 < x < \infty$, a > 0, then probability that x lies between x_1 and x_2 ($x_2 > x_1$) is

(a) $\left(e^{-ax_1} - e^{-ax_2}\right)$ (b) $a\left(e^{-ax_1} - e^{-ax_2}\right)$ (c) $e^{-ax_2}\left(e^{-ax_1} - e^{-ax_2}\right)$ (d) $e^{-ax_1}\left(e^{-ax_1} - e^{-ax_2}\right)$

62. If the partition function of a harmonic oscillator with frequency ω at a temperature T is $\frac{kT}{h\omega}$, then the free energy of N such independent oscillator is

(a)
$$\frac{3}{2}NkT$$
 (b) $kT\ln\frac{\hbar\omega}{kT}$ (c) $NkT\ln\frac{\hbar\omega}{kT}$ (d) $NkT\ln\frac{\hbar\omega}{2kT}$

63. The partition function of two Bose particles each of which can occupy any of the two energy levels 0 and ε is (a) $1 + e^{-2\varepsilon/kT} + 2e^{-\varepsilon/kT}$ (b) $1 + e^{-2\varepsilon/kT} + e^{-\varepsilon/kT}$

- (a) $1 + e^{-2\epsilon/kT} + 2e^{-\epsilon/kT}$ (b) $1 + e^{-\epsilon/kT} + e^{-\epsilon/kT}$ (c) $2 + e^{-2\epsilon/kT} + e^{-\epsilon/kT}$ (d) $e^{-2\epsilon/kT} + e^{-\epsilon/kT}$
- 64. A one dimensional random walker takes steps to left or right with equal probability. The probability that the random walker starting from origin is back to origin after *N* even number of steps is

(a)
$$\frac{N!}{\left(\frac{N}{2}\right)!\left(\frac{N}{2}\right)!}\left(\frac{1}{2}\right)^{N}$$
 (b) $\frac{N!\mathbf{D}}{\left(\frac{N}{2}\right)!\left(\frac{N}{2}\right)!}\mathbf{C}$ (c) $2N!\left(\frac{1}{2}\right)^{2N}$ (d) $N!\left(\frac{1}{2}\right)^{N}$

65. The number of states for a system of *N* identical free particles in a three dimensional space having total energy between *E* and $E + \delta E (\delta E \ll E)$, is proportional to

(a)
$$\left(E^{\frac{3N}{2}-1}\right)\delta E$$
 (b) $E^{N/2}\delta E$ (c) $NE^{1/2}\delta E$ (d) $E^N\delta E$

66. The energy of a ferromagnet as a function of magnetization M is given by

$$F(M) = F_0 + 2(T - T_c) M^2 + M^4, \quad F_0 > 0.$$

The number of minima in the function $F(M)$ for $T > T_c$ is
(a) 0 (b) 1 (c) 3 (d) 4



- **GATE-PH 2005 QUESTION PAPER** For a closed packed BCC structure of hard spheres, the lattice constant a is related to the sphere radius R as 67. (a) $a = \frac{4R}{\sqrt{2}}$ (b) $a = 4R\sqrt{3}$ (c) $a = 4R\sqrt{2}$ (d) $a = 2R\sqrt{2}$ An *n*-type semiconductor has an electron concentration of 3×10^{20} m⁻³. If the electron drift velocity is 100 68. ms⁻¹ in an electric field of 200 Vm⁻¹, the conductivity (in Ω^{-1} m⁻¹) of this material is (c) 48 (a) 24 (b) 36 (d) 96 Density of states of free electrons in a solid moving with an energy 0.1 eV is given by $2.15 \times 10^{21} \text{ eV}^{-1} \text{ cm}^{-3}$. 69. The density of states (in $eV^{-1}cm^{-3}$) for electrons moving with an energy of 0.4 eV will be (b) 1.52×10^{21} (c) 3.04×10^{21} (d) 4.30×10^{21} (a) 1.07×10^{21} The effective density of states at the conduction band edge of Ge is 1.04×10^{19} cm⁻³ at room temperature 70. (300 K). Ge has an optical bandgap of 0.66 eV. The intrinsic carrier concentration (in cm^{-3}) in Ge at room temperature (300 K) is approximately (c) 3×10^{16} (d) 3×10^{16} (b) 3×10^{13} (a) 3×10^{10} For a conventional superconductor, which of the following statements is NOT true? 71. (a) Specific heat is discontinuous at transition temperature T_c (b) The resistivity falls sharply at T_c (c) It is diamagnetic below T_c (d) It is paramagnetic below T_c 72. A nucleus having mass number 240 decays by α emission to the ground state of its daughter nucleus. The Q value of the process is 5.26 MeV. The energy (in MeV) of the α particle is (a) 5.26 (b) 5.17 (c) 5.13 (d) 5.09 The threshold temperature above which the thermonuclear reaction 73. ${}_{2}^{3}\text{He} + {}_{2}^{3}\text{He} \rightarrow {}_{2}^{4}\text{He} + {}_{1}^{1}\text{H} + 12.86 \text{ MeV} \text{ can occur is (use } e^{2/4\pi\epsilon_{0}} = 1.44 \times 10^{-15} \text{ MeVm})$ (a) 1.28×10^{10} K (b) 1.28×10^9 K (c) 1.28×10^8 K (d) 1.28×10^7 K According to the shell model, the ground state of $^{15}_{8}$ O nucleus is 74. (b) $\frac{1^{+}}{2}$ (a) $\frac{3^+}{2}$ (d) $\frac{1^{-}}{2}$ (c) $\frac{3^{-}}{2}$ 75. The plot of log A vs. time t, where A is activity, as shown in the figure, corresponds to decay Log A (a) from only one kind of radioactive nuclei having same half life (b) from only neutron activated nuclei
 - (c) from a mixture of radioactive nuclei having different half lives
 - (d) which is unphysical



76. For the rectifier circuit shown in the figure, the sinusoidal voltage $(V_1 \text{ or } V_2)$ at the output of the transformer has a maximum value of 10 V. The load resistance R_L is $k\Omega$. If I_{ave} is the average current through the resistor R_L the circuit corresponds



- (a) full wave rectifier with $I_{av} = 20/\pi \text{ mA}$
- (b) half wave rectifier with $I_{av} = 20/\pi$ mA

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- (c) half wave rectifier with $I_{av} = 10/\pi$ mA
- (d) full wave rectifier with $I_{av} = 10/\pi$ mA
- 77. The Boolean expression: B(A + B) + A. $(\overline{B} + A)$ can be realized using minimum number of (a) 1 AND gate (b) 2 AND gates (c) 1 OR gate (d) 2 OR gates
- 78. The output V_0 of the ideal opamp circuit shown in the figure is



80. In the circuit shown in the figure the Thevenin voltage V_{Th} and Thevenin resistance R_{Th} as seen by the load resistance R_L (=1 $k\Omega$) are respectively





81a.

81b.

82a.

82b.

QUESTION PAPER Linked Answer Questions : Q. 81a to Q. 85b carry two marks each. Statement for Linked Answer Q.81a and Q.81b : For the differential equation $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + y = 0$ One of the solutions is (c) e^{-x^2} (d) e^{x^2} (a) e^x (b) $\ln x$ The second linearly independent solution is (d) $x^2 e^{-x}$ (c) $x^2 e^x$ (b) xe^x (a) e^{-x} Statement for Linked Answer Q.82a and Q.82b : The Langrangian of two coupled oscillators of mass m each is $L = \frac{1}{2}m(x_1^2 + x_2^2) - \frac{1}{2}m\omega_0^2(x_1^2 + x_2^2) + m\omega_0^2\mu x_1 x_2$ The equation of motion are (a) $\ddot{x}_1 + \omega_0^2 \mu x_1$, $\ddot{x}_2 + \omega_0^2 x_2 = \omega_0^2 \mu x_2$ (b) $\ddot{x}_1 + \omega_0^2 x_2 - \omega_0^2 \mu x_1 = 0$, $\ddot{x}_2 + \omega_0^2 x_2 = \omega_0^2 \mu x_1$ (c) $\ddot{x}_1 + \omega_0^2 \mu x_1$, $\ddot{x}_2 + \omega_0^2 x_2 = -\omega_0^2 \mu x_2$ (d) $\ddot{x}_1 + \omega_0^2 \mu x_1$, $\ddot{x}_2 + \omega_0^2 x_2 = \omega_0^2 \mu x_1$ The normal modes of the system are (a) $\omega_0 \sqrt{\mu^2 - 1}, \omega_0 \sqrt{\mu^2 + 1}$ (b) $\omega_0 \sqrt{1-\mu^2}$, $\omega_0 \sqrt{1+\mu^2}$ (d) $\omega_0 \sqrt{1-\mu}, \, \omega_0 \sqrt{1+\mu}$ (c) $\omega_0 \sqrt{\mu - 1}, \, \omega_0 \sqrt{\mu + 1}$ Statement for Linked Answer Q.83a and Q.83b : An infinitely long hollow cylinder of radius R carrying a surface density σ is rotated about its cylindrical axis with a constant angular speed ω

- 83a. The magnitude of the surface current is
 - (a) $\sigma R^2 \omega$ (c) $\pi \sigma R \omega$ (d) $2\pi\sigma R\omega$ (b) $2\sigma R\omega$
- 83b. The magnitude of vector potential inside the cylindrical at a distance are from its axis is

(a)
$$2\mu_0 \sigma R \omega r$$
 (b) $\mu_0 \sigma R \omega r$ (c) $\frac{1}{2}\mu_0 \sigma R \omega r$ (d) $\frac{1}{4}\mu_0 \sigma R \omega r$

Statement for Linked Answer Q.84a and Q.84b :

A particle is scattered by a spherically symmetric potential. In the centre of mass (CM) frame the wavefunction of the incoming particle is $\psi = A e^{ikz}$, where k is the wavevector and A is a constant.

If $f(\theta)$ is an angular function then in the asymtotic region the scattered wavefunction has the form 84a.

(a)
$$\frac{A f(\theta) e^{ikr}}{r}$$
 (b) $\frac{A f(\theta) e^{-ikr}}{r}$ (c) $\frac{A f(\theta) e^{ikr}}{r^2}$ (d) $\frac{A f(\theta) e^{-ikr}}{r^2}$

- The differential scattering cross section $\sigma(\theta)$ in CM frame is 84b.
 - (a) $\sigma(\theta) = |A|^2 \frac{|f(\theta)|^2}{r^2}$ (b) $\sigma(\theta) = |A|^2 |f(\theta)|^2$
 - (c) $\sigma(\theta) = |f(\theta)|^2$ (d) $\sigma(\theta) = |A| |f(\theta)|$



QUESTION PAPER

Statement for Linked Answer Q.85(a) and Q.85(b) :

Lead has atomic weight of 207.2 amu and density of 11.35 gm cm^{-3}

- 85.a (A) Number of atoms per cm³ for lead is (a) 1.1×10^{25} (b) 3.3×10^{22} (c) 1.1×10^{22} (d) 3.3×10^{25}
- $\begin{array}{ll} \text{(B) If the energy of vacancy formation in lead is 0.55 eV/atom, the number of vacancies/cm³ at 500 K is \\ \text{(a) } 3.2 \times 10^{16} & \text{(b) } 3.2 \times 10^{19} & \text{(c) } 9.5 \times 10^{19} & \text{(d) } 9.5 \times 10^{16} \\ \end{array}$



