#### 1

#### PHYSICS-PH

Q.1 – Q.25: Carry ONE mark each.

- 1. A satellite is moving in a circular orbit around the Earth. If *T*, *V* and *E* are its average kinetic, average potential and total energies, respectively, then which one of the following options is correct?
  - (a) V = -2T: E = -T

(b) V = -T; E = 0

(c)  $V = \frac{-T}{2}$ ;  $E = \frac{T}{2}$ 

- (d)  $V = \frac{-3T}{2}$ ;  $E = \frac{-T}{2}$
- 2. The lattice parameters a, b, c of an orthorhombic crystal are related by a = 2b = 3c. In units of a, the interplanar separation between the (110) planes is \_\_\_\_\_ (upto three decimal places).
- 3. Consider w = f(z) = u(x, y) + iv(x, y) to be an analytic function in a domain *D*. Which one of the following options is NOT correct?
  - (a) u(x, y) satisfies Laplace equation in D
  - (b) v(x, y) satisfies Laplace equation in D
  - (c)  $\int_{z_1}^{z_2} f(z) dz$  is dependent on the choice of the contour between  $z_1$  and  $z_2$  in D
  - (d) f(z) can be Taylor expanded in D
- 4. Let  $\vec{L}$  and  $\vec{p}$  be the angular and linear momentum operators, respectively, for a particle. The commutator  $\begin{bmatrix} L_x, p_y \end{bmatrix}$  gives
  - (a)  $-i\hbar p_z$
- (b) 0
- (c)  $i\hbar p_x$
- (d)  $i\hbar p_z$
- 5. The dispersion relation for photons in a one dimensional monatomic Bravais lattice with lattice spacing a and consisting of ions of masses M is given by,  $\omega(k) = \sqrt{\frac{2C}{M}} \left[1 \cos{(ka)}\right]$ , where  $\omega$  is the frequency of oscillation, k is the wavevector and C is the spring constant. For the long wavelength modes  $(\lambda \gg a)$ , the ratio of the phase velocity to the group velocity is
- 6. For a black body radiation in a cavity, photons are created and annihilated freely as a result of emission and absorption by the walls of the cavity. This is because
  - (a) the chemical potential of the photons is zero
- (b) photons obey Pauli exclusion principle

(c) photons are spin-1 particles

- (d) the entropy of the photons is very large
- 7. Four forces are given below in Cartesian and spherical polar coordinates.
  - (i)  $\vec{F}_1 = K \exp\left(\frac{-r^2}{R^2}\right)\hat{r}$

(ii)  $\vec{F}_2 = K(x^3\hat{y} - y^3\hat{z})$ 

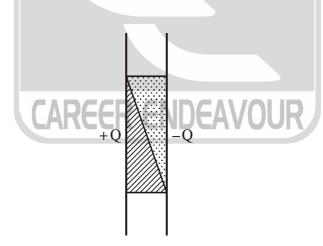
(iii)  $\vec{F}_3 = K\left(x^3\hat{x} + y^3\hat{y}\right)$ 

(iv)  $\vec{F}_4 = K \left( \frac{\hat{\phi}}{r} \right)$ 

where K is a constant. Identify the correct option.

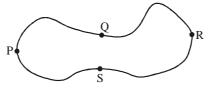
- (a) (iii) and (iv) are conservative but (i) and (ii) are not
- (b) (i) and (ii) are conservative but (iii) and (iv) are not
- (c) (ii) and (iii) are conservative but (i) and (iv) are not
- (d) (i) and (iii) are conservative but (ii) and (iv) are not

- The value of  $\int_0^3 t^2 \delta(3t 6) dt$  is\_\_\_\_\_ (upto one decimal place) 8.
- The mean kinetic energy of a nucleon in a nucleus of atomic weight A varies as  $A^n$ , where n is \_\_\_\_\_ (upto 9. two decimal places)
- 10. In Bose-Einstein condensates, the particles
  - (a) have strong interparticle attraction
- (b) condense in real space
- (c) have overlapping wavefunctions
- (d) have large and positive chemical potential
- A beam of X-ray of intensity I<sub>0</sub> is incident normally on a metal sheet of thickness 2 mm. The intensity of the 11. transmitted beam is 0.025I<sub>0</sub>. The linear absorption coefficient of the metal sheet (in m<sup>1</sup>) is \_\_\_\_\_ (upto one decimal place)
- 12. In a Hall effect experiment, the Hall voltage for an intrinsic semiconductor is negative. This is because (symbols carry usual meaning)
  - (a)  $n \approx p$
- (b) n > p
- (c)  $\mu_{e} > \mu_{h}$  (d)  $m_{e}^{*} > m_{h}^{*}$
- The Pauli matrices for three spin- $\frac{1}{2}$  particles are  $\vec{\sigma}_1$ ,  $\vec{\sigma}_2$  and  $\vec{\sigma}_3$ , respectively. The dimension of the Hilbert 13. space required to define an operator  $\hat{O} = \vec{\sigma}_1 \cdot \vec{\sigma}_2 \times \vec{\sigma}_3$  is\_\_\_
- 14. The decay  $\mu^+ \rightarrow e^+ + \gamma$  is forbidden, because it violates
  - (a) momentum and lepton number conservations
  - (b) baryon and lepton number conservations
  - (c) angular momentum conservation
  - (d) lepton number conservation
- 15. The space between two plates of a capacitor carrying charges +Q and –Q is filled with two different dielectric materials, as shown in the figure. Across the interface of the two dielectric materials, which one of the following statements is correct?

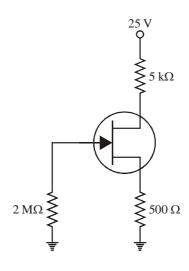


- (a)  $\vec{E}$  and  $\vec{D}$  are continuous
- (b)  $\vec{E}$  is continuous and  $\vec{D}$  is discontinuous
- (c)  $\vec{D}$  is continuous and  $\vec{E}$  is discontinuous
- (d)  $\vec{E}$  and  $\vec{D}$  are discontinuous

16. Given that magnetic flux through the closed loop PQRSP is  $\phi$ . If  $\int_{P}^{R} \vec{A} \cdot \vec{dl} = \phi_1$  along PQR, the value of  $\int_{P}^{R} \vec{A} \cdot \vec{dl}$  along PSR is



- (a)  $\phi \phi_1$
- (b)  $\phi_1 \phi$
- $(c) \phi_1$
- (d)  $\phi_1$
- 17. A point charge is placed between two semi-infinite conducting plates which are inclined at an angle of 30° with respect to each other. The number of image charges is\_\_\_\_\_
- 18. Consider a complex function  $f(z) = \frac{1}{z\left(z + \frac{1}{2}\right)\cos(z\pi)}$ . Which one of the following statements is correct?
  - (a) f(z) has simple poles at z = 0 and  $z = -\frac{1}{2}$
  - (b) f(z) has a second order pole at  $z = -\frac{1}{2}$
  - (c) f(z) has infinite number of second order poles
  - (d) f(z) has all simple poles
- 19. The energy dependence of the density of states for a two dimensional non-relativistic electron gas is given by,  $g(E) = CE^n$ , where *C* is constant. The value of *n* is \_\_\_\_\_\_
- 20. In an inertial frame S, two events A and B take place at  $(ct_A = 0, \vec{r}_A = 0)$  and  $(ct_B = 0, \vec{r}_B = 2\hat{y})$ , respectively. The times at which these events take place in a frame S' moving with a velocity  $0.6 c \hat{y}$  with respect to S are given by
  - (a)  $ct'_A = 0$ ;  $ct'_B = -3/2$
- (b)  $ct'_A = 0$ ;  $ct'_B = 0$ (d)  $ct'_A = 0$ ;  $ct'_B = 1/2$
- (c)  $c t'_A = 0$ ;  $c t'_B = 3/2$
- 21. In the given circuit, the voltage across the source resistor is 1 V. The drain voltage (in V) is \_\_\_\_\_\_



- If  $f(x) = e^{-x^2}$  and  $g(x) = |x|e^{-x^2}$ , then 22.
  - (a) f and g are differentiable everywhere
  - (b) f is differentiable everywhere but g is not
  - (c) g is differentiable everywhere but f is not
  - (d) g is discontinuous at x = 0
- Consider a system of N non-interacting spin- $\frac{1}{2}$  particles, each having a magnetic moment  $\mu$ , is in a magnetic 23.

field  $\vec{B} = B \hat{z}$ . If E is the total energy of the system, the number of accessible microstates  $\Omega$  is given by

(a) 
$$\Omega = \frac{N!}{\frac{1}{2} \left( N - \frac{E}{\mu B} \right)!}$$
 (b)  $\Omega = \frac{\left( N - \frac{E}{\mu B} \right)!}{\left( N + \frac{E}{\mu B} \right)!}$ 

(b) 
$$\Omega = \frac{\left(N - \frac{E}{\mu B}\right)!}{\left(N + \frac{E}{\mu B}\right)!}$$

(c) 
$$\Omega = \frac{1}{2} \left( N - \frac{E}{\mu B} \right)! \frac{1}{2} \left( N + \frac{E}{\mu B} \right)!$$

(d) 
$$\Omega = \frac{N!}{\left(N + \frac{E}{\mu B}\right)!}$$

- 24. Which one of the following DOES NOT represent an exclusive OR operation for inputs A and B?
  - (a)  $(A+B)\overline{AB}$
- (b)  $A\overline{B} + B\overline{A}$
- (c)  $(A+B)(\overline{A}+\overline{B})$  (d) (A+B)AB
- An operator for a spin- $\frac{1}{2}$  particle is given by  $\hat{A} = \lambda \vec{\sigma} \cdot \vec{B}$ , where  $\vec{B} = \frac{B}{\sqrt{2}} (\hat{x} + \hat{y})$ ,  $\vec{\sigma}$  denotes Pauli matrices 25.

and  $\lambda$  is a constant. The eigenvalue of  $\hat{A}$  are

(a) 
$$\frac{\pm \lambda B}{\sqrt{2}}$$

- (b)  $\pm \lambda B$
- (c)  $0, \lambda B$
- (d)  $0, -\lambda B$

# Q.26 – Q.55 : Carry TWO marks each.

26. Match the phrases in **Group I** and **Group II** and identify the correct option.

### Group I

# **Group II**

- (P) Electron spin resonance (ESR)
- (Q) Nuclear magnetic resonance (NMR)
- (R) Transition between vibrational states of a molecule
- (ii) visible range frequency (iii) microwave frequency

(S) Electronic transition

(iv) far-infrared range

(i) radio frequency

- (a) (P-i), (Q-ii), (R-iii), (S-iv)
- (b) (P-ii), (Q-i), (R-iv), (S-iii)
- (c) (P-iii), (Q-iv), (R-i), (S-ii)
- (d) (P-iii), (Q-i), (R-iv), (S-ii)
- The entropy of a gas containing N particles enclosed in a volume V is given by  $S = Nk_B \ln \left( \frac{aVE^{3/2}}{N^{5/2}} \right)$ , where 27.

E is the total energy, a is a constant and  $k_B$  is the Boltzmann constant. The chemical potential  $\mu$  of the system at a temperature T is given by

(a) 
$$\mu = -k_B T \left[ \ell n \left( \frac{aV E^{3/2}}{N^{5/2}} \right) - \frac{5}{2} \right]$$

(b) 
$$\mu = -k_B T \left[ \ell n \left( \frac{aV E^{3/2}}{N^{5/2}} \right) - \frac{3}{2} \right]$$

(c) 
$$\mu = -k_B T \left[ \ell n \left( \frac{aV E^{3/2}}{N^{3/2}} \right) - \frac{5}{2} \right]$$

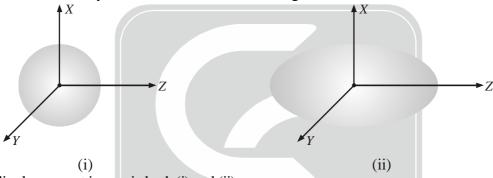
(d) 
$$\mu = -k_B T \left[ \ell n \left( \frac{aV E^{3/2}}{N^{3/2}} \right) - \frac{3}{2} \right]$$

- The atomic masses of  ${}^{152}_{63}Eu$ ,  ${}^{152}_{62}Sm$ ,  ${}^{1}_{1}H$  and neutron are 151.921749, 151.919756, 1.007825 and 1.008665 28. in atomic mass units (amu), respectively. Using the above information, the O-value of the reaction  $^{152}_{63}Eu + n \rightarrow ^{152}_{62}Sm + p \text{ is} \_\_\_ \times 10^{-3} \text{ amu (upto three decimal places)}$
- A particle with rest mass M is at rest and decays into two particles of equal rest masses  $\frac{3}{10}M$  which move 29. along the z-axis. Their velocities are given by
  - (a)  $\vec{v}_1 = \vec{v}_2 = (0.8c)\hat{z}$

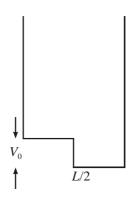
(b)  $\vec{v}_1 = -\vec{v}_2 = (0.8c)\hat{z}$ 

(c)  $\vec{v}_1 = -\vec{v}_2 = (0.6c)\hat{z}$ 

- (d)  $\vec{v}_1 = (0.6c)\hat{z}$ ;  $\vec{v}_2 = (-0.8c)\hat{z}$
- The band gap of an intrinsic semiconductor is  $E_g = 0.72 \ eV$  and  $m_h^* = 6 m_e^*$ . At 300K, the Fermi level with 30. respect to the edge of the valence band (in eV) is at \_\_\_\_\_ (upto three decimal places)  $k_R = 1.38 \times 10^{-23} \ JK^{-1}$ .
- A charge -q is distributed uniformly over a sphere, with a positive charge q at its center in (i). Also in (ii), a 31. charge -q is distributed uniformly over an ellipsoid with a positive charge q at its center. With respect to the origin of the coordinate system, which one of the following statements is correct?



- (a) The dipole moment is zero in both (i) and (ii)
- (b) The dipole moment is non-zero in (i) but zero in (ii)
- (c) The dipole moment is zero in (i) but non-zero in (ii)
- (d) The dipole moment is non-zero in both (i) and (ii)
- The number of permitted transitions from  ${}^2P_{3/2} \rightarrow {}^2S_{1/2}$  in the presence of a weak magnetic field is 32.
- A particle is confined in a box of length L as shown below 33.



If the potential  $V_0$  is treated as a perturbation, including the first order correction, the ground state energy is

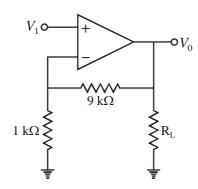
(a) 
$$E = \frac{\hbar^2 \pi^2}{2mI^2} + V_0$$

(b) 
$$E = \frac{\hbar^2 \pi^2}{2mL^2} - \frac{V_0}{2}$$

(c) 
$$E = \frac{\hbar^2 \pi^2}{2mI^2} + \frac{V_0}{4}$$

(a) 
$$E = \frac{\hbar^2 \pi^2}{2mL^2} + V_0$$
 (b)  $E = \frac{\hbar^2 \pi^2}{2mL^2} - \frac{V_0}{2}$  (c)  $E = \frac{\hbar^2 \pi^2}{2mL^2} + \frac{V_0}{4}$  (d)  $E = \frac{\hbar^2 \pi^2}{2mL^2} + \frac{V_0}{2}$ 

34. In the given circuit, if the open loop gain  $A = 10^5$ , the feedback configuration and the closed loop gain  $A_f$  are



(a) series-shunt,  $A_f = 9$ (c) series-shunt,  $A_f = 10$ 

- (b) series-series,  $A_f = 10$ (d) shunt-shunt,  $A_f = 10$
- A plane wave  $(\hat{x} + i\hat{y})E_0 \exp[i(kz \omega t)]$  after passing through an optical element emerges as 35.  $(\hat{x} - i\hat{y})E_0 \exp[i(kz - \omega t)]$ , where k and  $\omega$  are the wavevector and the angular frequency, respectively. The optical element is
  - (a) quarter wave plate

(b) half wave plate

(c) polarizer

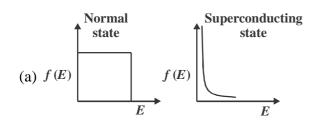
- (d) Faraday rotator
- A particle of mass 0.01 kg falls freely in the earth's gravitational field with an initial velocity  $v(0) = 10 \, ms^{-1}$ . If 36. the air exerts a functional force of the form, f = -kv, then for  $k = 0.05 \, Nm^{-1}s$ , the velocity (in  $ms^{-1}$ ) at time t = 0.2 s is\_\_\_\_\_ (upto two decimal places) (use  $g = 10 ms^{-2}$  and e = 2.72)
- The Lagrangian for a particle of mass m at a position  $\vec{r}$  moving with a velocity  $\vec{v}$  is given by 37.  $L = \frac{m}{2}\vec{v}^2 + C\vec{r}\cdot\vec{v} - V(r)$ , where V(r) is a potential and C is a constant. If  $\vec{p}_c$  is the canonical momentum, then its Hamiltonian is given by

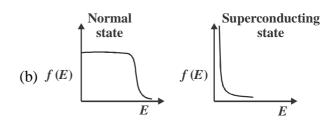
  - (a)  $\frac{1}{2m} (\vec{p}_c + C\vec{r})^2 + V(r)$ (b)  $\frac{1}{2m} (\vec{p}_c C\vec{r})^2 + V(r)$ (c)  $\frac{1}{2m} (\vec{p}_c C\vec{r})^2 + V(r)$ (d)  $\frac{1}{2m} p_c^2 + C^2 r^2 + V(r)$
  - (c)  $\frac{p_c^2}{2m} + V(r)$

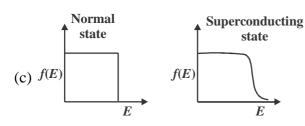
- 38. A long solenoid is embedded in a conducting medium and is insulated from the medium. If the current through the solenoid is increased at a constant rate, the induced current in the medium as a function of the radial distance r from the axis of the solenoid is proportional to

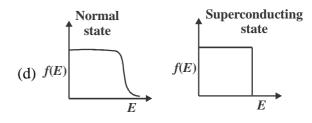
  - (a)  $r^2$  inside the solenoid and  $\frac{1}{r}$  outside (b) r inside the solenoid and  $\frac{1}{r^2}$  outside
  - (c)  $r^2$  inside the solenoid and  $\frac{1}{r^2}$  outside (d) r inside the solenoid and  $\frac{1}{r}$  outside
- In the nuclear shell model, the potential is modeled as  $V(r) = \frac{1}{2}m\omega^2r^2 \lambda\vec{L}\cdot\vec{S}$ ,  $\lambda > 0$ . The correct spin-39. parity and isospin assignments for the ground state of  ${}^{13}C$  is
  - (a)  $\frac{1}{2}$ ;  $\frac{-1}{2}$
- (b)  $\frac{1^{+}}{2}$ ;  $\frac{-1}{2}$
- (c)  $\frac{3^+}{2}$ ;  $\frac{1}{2}$  (d)  $\frac{3^-}{2}$ ;  $\frac{-1}{2}$

40. Which one of the following represents the electron occupancy for a superconductor in its normal and superconducting states?









- 41. In a rigid-rotator of mass M, if the energy of the first excited state is 1 meV, then the fourth excited state energy (in meV) is\_\_\_\_\_
- 42. The binding energy per molecule of NaCl (lattice parameter is 0.563 nm) is 7.95 eV. The repulsive term of the potential is of the form  $\frac{K}{r^9}$ , where K is a constant. The value of the Madelung constant is \_\_\_\_\_\_(upto three decimal places)

(Electron charge  $e = 1.6 \times 10^{-19} C$ ;  $\varepsilon_0 = 8.854 \times 10^{-12} C^2 N^{-1} m^{-2}$ )

- 43. The Hamiltonian for a system of two particles of masses  $m_1$  and  $m_2$  at  $\vec{r_1}$  and  $\vec{r_2}$  having velocities  $\vec{v_1}$  and  $\vec{v_2}$  is given by  $H = \frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2 + \frac{C}{\left(\vec{r_1} \vec{r_2}\right)^2}\hat{z} \cdot \left(\vec{r_1} \times \vec{r_2}\right)$ , where C is a constant. Which one of the following statements is correct?
  - (a) The total energy and total momentum are conserved
  - (b) Only the total energy is conserved
  - (c) The total energy and the z-component of the total angular momentum are conserved
  - (d) The total energy and total angular momentum are conserved
- 44. Given that the Fermi energy of gold is 5.54 eV, the number density of electrons is \_\_\_\_\_\_× $10^{28}$  m<sup>-3</sup> (upto one decimal place). (Mass of electron =  $9.11 \times 10^{-21}$  kg; h =  $6.626 \times 10^{-24}$ J.s; 1 eV =  $1.6 \times 10^{-19}$  J)
- 45. Suppose a linear harmonic oscillator of frequency  $\omega$  and mass m is in the state  $|\psi\rangle = \frac{1}{\sqrt{2}} \left[ |\psi_0\rangle + e^{i\frac{\pi}{2}} |\psi_1\rangle \right]$  at t = 0 where  $|\psi_0\rangle$  and  $|\psi_1\rangle$  are the ground and the first excited states, respectively. The value of  $\langle \psi | x | \psi \rangle$  in the units of  $\sqrt{\frac{\hbar}{m\omega}}$  at t = 0 is \_\_\_\_\_\_

- Consider the motion of the Sun with respect to the rotation of the Earth about its axis. If  $\vec{F}_c$  and  $\vec{F}_{Co}$  denote the 46. centrifugal and the Coriolis forces, respectively, acting on the Sun, then

  - (a)  $\vec{F}_c$  is radially outward and  $\vec{F}_{Co} = \vec{F}_c$  (b)  $\vec{F}_c$  is radially inward and  $\vec{F}_{Co} = -2\vec{F}_c$
  - (c)  $\vec{F}_c$  is radially outward and  $\vec{F}_{Co} = -2\vec{F}_c$  (d)  $\vec{F}_c$  is radially outward and  $\vec{F}_{Co} = 2\vec{F}_c$
- A function y(z) satisfies the ordinary differential equation  $y'' + \frac{1}{z}y' \frac{m^2}{z^2}y = 0$ , where m = 0, 1, 2, 3, ...47.

Consider the four statements P, Q, R, S as given below.

 $P: z^m$  and  $z^{-m}$  are linearly independent solutions for all values of m

 $Q: z^m$  and  $z^{-m}$  are linearly independent solutions for all values of m > 0

 $R: \ell n \ z$  and 1 are linearly independent solutions for m=0

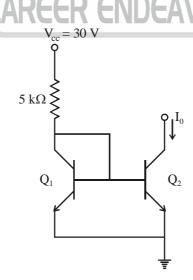
 $S: z^m$  and  $\ell n z$  are linearly independent solutions for all values of m

The correct option for the combination of valid statement is

- (a) P, R and S only
- (b) P and R only
- (c) Q and R only
- (d) R and S only
- 48. The average energy U of a one dimensional quantum oscillator of frequency  $\omega$  and in contact with a heat bath at temperature T is given by
  - (a)  $U = \frac{1}{2}\hbar\omega \coth\left(\frac{1}{2}\beta\hbar\omega\right)$
- (b)  $U = \frac{1}{2}\hbar\omega \sinh\left(\frac{1}{2}\beta\hbar\omega\right)$
- (c)  $U = \frac{1}{2}\hbar\omega \tanh\left(\frac{1}{2}\beta\hbar\omega\right)$
- (d)  $U = \frac{1}{2}\hbar\omega \cosh\left(\frac{1}{2}\beta\hbar\omega\right)$
- Consider a system of eight non-interacting, identical quantum particles of spin- $\frac{3}{2}$  in a one dimensional box of 49.

length L. The minimum excitation energy of the system, in units of  $\frac{\pi^2 \hbar^2}{2mL^2}$  is\_\_\_\_\_\_

In the simple current source shown in the figure,  $Q_1$  and  $Q_2$  are identical transistors with current gain 50.  $\beta = 100 \text{ and } V_{BE} = 0.7 V$ 



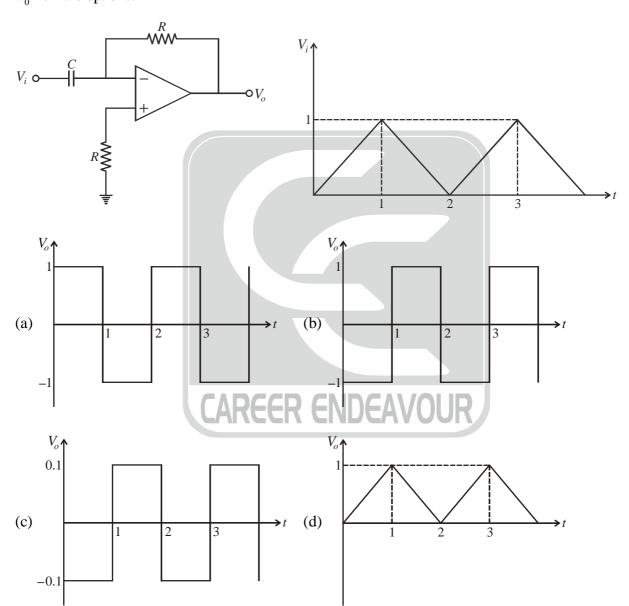
The current I<sub>0</sub> (in mA) is \_\_\_\_\_(upto two decimal places)



The Heaviside function is defined as  $H(t) = \begin{cases} +1 & \text{for } t > 0 \\ -1 & \text{for } t < 0 \end{cases}$  and its Fourier transform is given by  $-2i/\omega$ . The 51.

Fourier transform of  $\frac{1}{2} \left[ H\left(t + \frac{1}{2}\right) - H\left(t - \frac{1}{2}\right) \right]$  is

- (a)  $\frac{\sin\left(\frac{\omega}{2}\right)}{\frac{\omega}{2}}$  (b)  $\frac{\cos\left(\frac{\omega}{2}\right)}{\frac{\omega}{2}}$  (c)  $\sin\left(\frac{\omega}{2}\right)$
- (d) 0
- Consider the circuit shown in the figure, where RC = 1. For an input signal  $V_i$  shown below, choose the correct 52.  $V_0$  from the options:



- 53. Let the Hamiltonian for two spin- $\frac{1}{2}$  particles of equal masses m, momenta  $\vec{p}_1$  and  $\vec{p}_2$  and positions  $\vec{r}_1$  and  $\vec{r}_2$  be  $H = \frac{1}{2m} p_1^2 + \frac{1}{2m} p_2^2 + \frac{1}{2} m \omega^2 \left( r_1^2 + r_2^2 \right) + k \vec{\sigma}_1 \cdot \vec{\sigma}_2$ , where  $\vec{\sigma}_1$  and  $\vec{\sigma}_2$  denote the corresponding Pauli matrices,  $\hbar \omega = 0.1 \, eV$  and  $k = 0.2 \, eV$ . If the ground state has net spin zero, then the energy (in eV) is
- 54. The excitation wavelength of laser in a Raman effect experiment is  $546 \, nm$ . If the Stokes line is observed at  $552 \, nm$ , then the wave number of the anti-Stokes line (in  $cm^{-1}$ ) is\_\_\_\_\_
- 55. A monochromatic plane wave (wavelength = 600 nm)  $E_0 \exp \left[i(kz \omega t)\right]$  is incident normally on a diffraction grating giving rise to a plane wave  $E_1 \exp \left[i(\vec{k_1} \cdot \vec{r} \omega t)\right]$  in the first order of diffraction. Here  $E_1 < E_0$  and  $\vec{k_1} = \left|\vec{k_1}\right| \left[\frac{1}{2}\hat{x} + \frac{\sqrt{3}}{2}\hat{z}\right]$ . The period (in  $\mu m$ ) of the diffraction grating is \_\_\_\_\_ (upto one decimal place)

