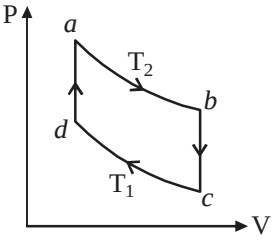
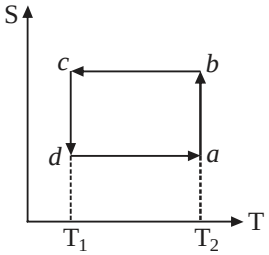
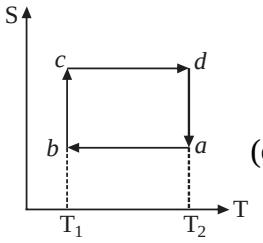
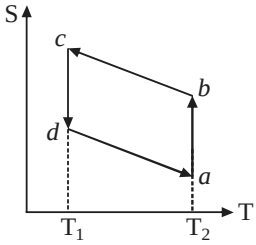
PHYSICS-PH

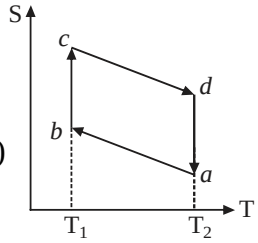
11. Which one of the following entropy (S) - temperature (T) diagrams CORRECTLY represents the Carnot cycle *abcda* shown in the P-V diagram?



(a) 

(b) 

(c) 

(d) 

12. Which one of the following is a dimensionless constant?
(a) Permittivity of free space (b) Permeability of free space
(c) Bohr magneton (d) Fine structure constant

13. Choose the most appropriate matching of the items in Column 1 with those in Column 2.

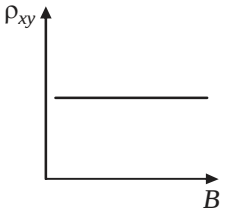
Column-1	**Column-2**
(i) PIN diode	P. Voltage regulation
(ii) Tunnel diode	Q. Radio frequency and microwave devices
(iii) Zener diode	R. Optoelectronic detection
(iv) Photo diode	S. Oscillator

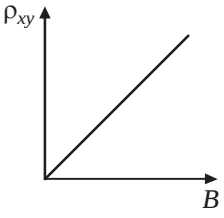
(a) (i) - Q; (ii) - S; (iii) - P; (iv) - R (b) (i) - R; (ii) - Q; (iii) - P; (iv) - S
(c) (i) - R; (ii) - S; (iii) - P; (iv) - Q (d) (i) - P; (ii) - Q; (iii) - R; (iv) - S

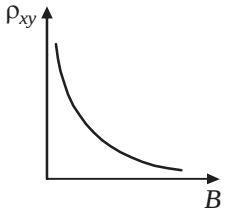
14. The atomic number of an atom is 6. What is the spectroscopic notation of its ground state, according to Hund's rules?
(a) $^3P_0$ (b) $^3P_1$ (c) $^3D_3$ (d) $^3S_1$

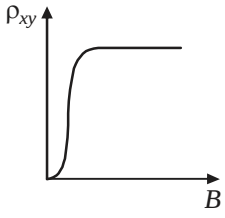
15. H is the Hamiltonian, $\vec{L}$ the orbital angular momentum and L_z is the z-component of $\vec{L}$. The 1s state of the hydrogen atom in the non-relativistic formalism is an eigen function of which one of the following sets of operators?
(a) H, L^2 and L_z (b) $H, \vec{L}, L^2$ and L_z (c) L^2 and L_z only (d) H and L_z only

16. The Hall experiment is carried out with a non-magnetic semiconductor. The current I is along the x-axis and the magnetic field B is along the z-axis. Which one of the following is the CORRECT representation of the variation of the magnitude of the Hall resistivity ρ_{xy} as a function of the magnetic field?

(a) 

(b) 

(c) 

(d) 

17. Consider a two dimensional Cartesian coordinate system in which a rank 2 contravariant tensor is represented by the matrix

$$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

The coordinate system is rotated anticlockwise by an acute angle θ with the origin fixed. Which one of the following matrices represents the tensor in the new coordinate system?

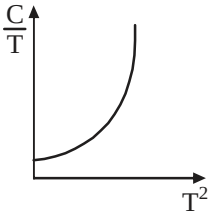
(a) $\begin{pmatrix} 0 & \cos 2\theta \\ -\sin 2\theta & 0 \end{pmatrix}$ (b) $\begin{pmatrix} \sin 2\theta & \cos 2\theta \\ \cos 2\theta & -\sin 2\theta \end{pmatrix}$

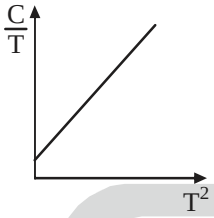
(c) $\begin{pmatrix} \sin 2\theta & -\cos 2\theta \\ \cos 2\theta & \sin 2\theta \end{pmatrix}$ (d) $\begin{pmatrix} \sin 2\theta & 0 \\ 0 & -\cos 2\theta \end{pmatrix}$

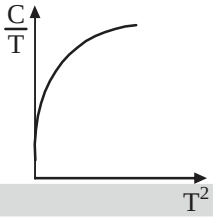
18. A compound consists of three ions X, Y and Z. The Z ions are arranged in an FCC arrangement. The X ions occupy 1/6 of the tetrahedral voids and the Y ions occupy 1/3 of the octahedral voids. Which one of the following is the CORRECT chemical formula of the compound?

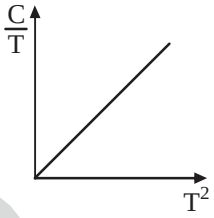
(a) XY_2Z_4 (b) XYZ_3 (c) XYZ_2 (d) XYZ_4

19. For a non-magnetic metal, which one of the following graphs best represents the behaviour of C/T vs. T^2, where C is the heat capacity and T is the temperature?

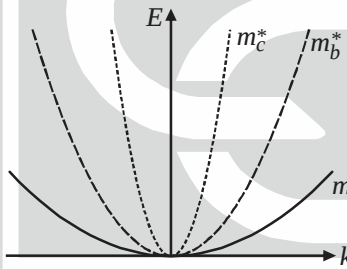
(a) 

(b) 

(c) 

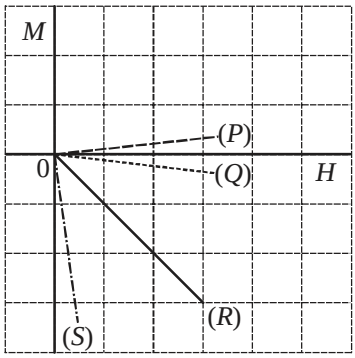
(d) 

20. For nonrelativistic electrons in a solid, different energy dispersion relations (with effective masses m_a^*, m_b^* and m_c^*) are schematically shown in the plots. Which one of the following options is CORRECT?



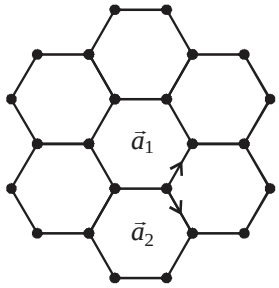
(a) $m_a^* = m_b^* = m_c^*$ (b) $m_b^* > m_c^* > m_a^*$ (c) $m_c^* > m_b^* > m_a^*$ (d) $m_a^* > m_b^* > m_c^*$

21. The figure schematically shows the M (magnetization) - H (magnetic field) plots for certain types of materials. Here M and H are plotted in the same scale and units. Which one of the following is the most appropriate combination?



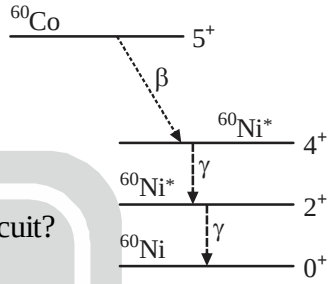
(a) (Q) - Paramagnet; (R) - Type-I Superconductor; (S) - Antiferromagnet
(b) (P) - Paramagnet; (Q) - Diamagnet; (R) - Type-I Superconductor
(c) (P) - Paramagnet; (Q) - Antiferromagnet; (R) - Type-I Superconductor
(d) (P) - Diamagnet; (R) - Paramagnet; (S) - Type-I Superconductor

22. Graphene is a two dimensional material, in which carbon atoms are arranged in a honeycomb lattice with lattice constant a. As shown in the figure, $\vec{a}_1$ and $\vec{a}_2$ are two lattice vectors. Which one of the following is the area of the first Brillouin zone for this lattice?



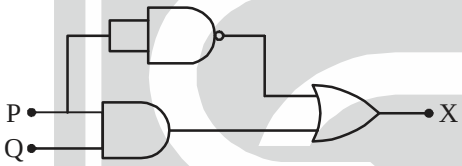
(a) $\frac{8\pi^2}{3\sqrt{3}a^2}$ (b) $\frac{4\pi^2}{3\sqrt{3}a^2}$ (c) $\frac{8\pi^2}{\sqrt{3}a^2}$ (d) $\frac{4\pi^2}{\sqrt{3}a^2}$

23. A ^{60}Co nucleus emits a β -particle and is conserved to ^{60}Ni* with $J^P = 4^+$, which in turn decays to the ^{60}Ni ground state with $J^P = 0^+$ by emitting two photons in succession, as shown in the figure. Which one of the following statements is CORRECT?



(a) $4^+ \rightarrow 2^+$ is an electric octupole transition.
(b) $4^+ \rightarrow 2^+$ is a magnetic quadrupole transition.
(c) $2^+ \rightarrow 0^+$ is an electric quadrupole transition.
(d) $2^+ \rightarrow 0^+$ is magnetic quadrupole transition.

24. Which one of the following options is CORRECT for the given logic circuit?



(a) P = 1, Q = 1; X = 0 (b) P = 1, Q = 0; X = 1
(c) P = 0, Q = 1; X = 0 (d) P = 0, Q = 0; X = 1

25. An atom with non-zero magnetic moment has an angular momentum of magnitude $\sqrt{12}\hbar$. When a beam of such atoms is passed through a Stern-Gerlach apparatus, how many beams does it split into?
(a) 3 (b) 7 (c) 9 (d) 25

26. A 4×4 matrix M has the property $M^\dagger = -M$ and $M^4 = 1$, where 1 is the 4×4 identity matrix. Which one of the following is the CORRECT set of eigenvalues of the matrix M?
(a) $(1, 1, -1, -1)$ (b) $(i, i, -i, -i)$ (c) $(i, i, i, -i)$ (d) $(1, 1, -i, -i)$

27. The Ξ^{0*} particle is a member of the Baryon decuplet with isospin state $|I, I_3\rangle = \left|\frac{1}{2}, \frac{1}{2}\right\rangle$ and strangeness quantum number –2. In the quark mode, which one of the following is the flavour part of the Ξ^{0*} wavefunction?

(a) $\frac{1}{\sqrt{2}}(uss - ssu)$ (b) $\frac{1}{\sqrt{3}}(uss + sus + ssu)$

(c) $\frac{1}{\sqrt{2}}(uss + ssu)$ (d) $\frac{1}{\sqrt{3}}(uss - sus + ssu)$

28. Which of the following is(are) the CORRECT option(s) for the Joule-Thomson effect?
(a) It is an isentropic process. (b) It is an isenthalpic process.
(c) It can result in cooling as well as heating. (d) For an ideal gas it always results in cooling

29. The deuteron is a bound state of a neutron and a proton. Which of the following statements is(are) CORRECT?
(a) The deuteron has a finite value of electric quadrupole moment due to non-spherical electronic charge distribution.
(b) The magnetic moment of the deuteron is equal to the sum of the magnetic moments of the neutron and the proton.
(c) The deuteron state is an admixture of $^3S_1$ and $^3D_1$ states.
(d) The deuteron state is an admixture of $^3S_1$ and $^3P_1$ states.

30. The Geiger-Muller counter is a device to detect α, β and γ radiations. It is a cylindrical tube filled with monatomic gases like argon, and polyatomic gases such as ethyl alcohol. The inner electrode is along the axis of the cylindrical tube and the outer electrode is the tube. Which of the following statements is(are) CORRECT?
(a) Argon is used so that ambient light coming from the surroundings do not produce any signal in the detector.
(b) Ethyl alcohol is used as a quenching gas.
(c) The electric field strength decreases from the axis to the edge of the tube and the direction of the field is radially outward.
(d) The electric field increases from the axis to the edge of the tube and the field direction is radially inward.

31. Consider an isolated magnetized sphere of radius R with a uniform magnetization $\vec{M}$ along the positive z direction, with the north and south poles of the sphere lying on the z-axis. It is given that the magnetic field inside the sphere is $\vec{B} = \frac{2\mu_0}{3}\vec{M}$, where μ_0 is the permeability of vacuum. Which of the following statements is(are) CORRECT?
(a) The bound volume current density is zero.
(b) The bound surface current density has maximum magnitude at the equator, where this magnitude equals $\left|\vec{M}\right|$.
(c) The auxiliary field $\vec{H} = -\frac{2}{3}\vec{M}$.
(d) Far from the sphere, the magnetic field is due to a dipole of moment $\vec{m}$, where $\frac{\vec{m}}{4\pi R^3} = \frac{B}{2\mu_0}\hat{z}$.

32. Which of the following options represent(s) linearly independent pair(s) of functions of a real variable x?
(a) e^{ix} and e^{-ix} (b) x and e^x (c) 2^x and 2^{-3+x} (d) e^{ix} and $\sin x$

33. In the vector model of angular momentum applied to atoms, what is the minimum angle in degrees (in integer) made by the orbital angular momentum vector and the positive z-axis for a 2p electron ?

34. For a transistor amplifier, the frequency response is such that the mid band voltage gain is 200. The cutoff frequencies are 20 Hz and 20 kHz. What is the ratio (rounded off to two decimal places) of the voltage gain at 10 Hz to that at 100 kHz ?

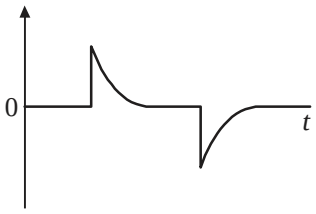
35. An electric field as a function of radial coordinate r has the form $\vec{E} = \alpha\frac{e^{-r^2}}{r}\hat{r}$, where α is a constant. Assume that dimensions are appropriately taken care of. The electric flux through a sphere of radius $\sqrt{2}$, centered at the origin, is ϕ. What is the value of $\frac{\phi}{2\pi\alpha}$ (Rounded off to two decimal places) ?

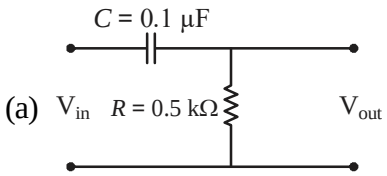
Q.36 – Q.65 Carry Two marks each.

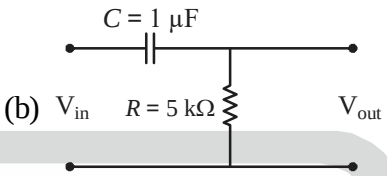
36. It is given that the electronic ground state of a diatomic molecule X_2 has even parity and the nuclear spin of X is 0. Which one of the following is the CORRECT statement with regard to the rotational Raman spectrum (J is the rotational quantum number) of this molecule?

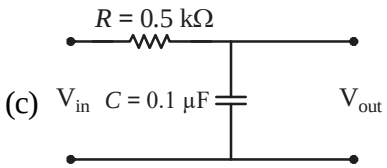
(a) Lines of all J values are present.
(b) Lines have alternating intensity in the ratio of 3 : 1.
(c) Lines of only even J values are present.
(d) Lines of only odd J values are present.

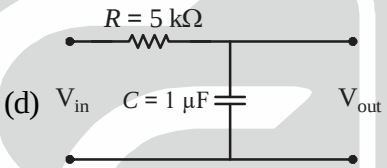
37. An input voltage in the form of a square wave of frequency 1 kHz is given to a circuit, which results in the output shown schematically below. Which one of the following options is the CORRECT representation of the circuit?











38. A simple harmonic oscillator with an angular frequency ω is in thermal equilibrium with a reservoir at absolute temperature T, with $\omega = \frac{2k_BT}{\hbar}$. Which one of the following is the partition function of the system ?

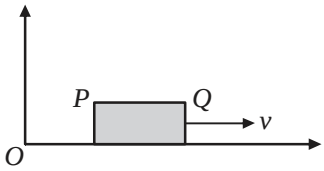
(a) $\frac{e}{e^2-1}$ (b) $\frac{e}{e^2+1}$ (c) $\frac{e}{e-1}$ (d) $\frac{e}{e+1}$

39. Which one of the following options is the most appropriate match between the items given in Column 1 and Column 2?

Column 1	Column 2
(i) Visible light	P. Transition between core energy levels of atoms
(ii) X-rays	Q. Transition between nuclear energy levels
(iii) Gamma rays	R. Pair production
(iv) Thermal neutrons	S. Crystal structure determination
	T. Photoelectric effect

(a) (i) - T; (ii) - P,S,T; (iii) - Q,R; (iv) - S
(b) (i) - P,T; (ii) - S; (iii) - R,S; (iv) - S,T
(c) (i) - T; (ii) - R,S; (iii) - Q,R; (iv) - S
(d) (i) - S,T; (ii) - P,S; (iii) - R,T; (iv) - S

40. A rod PQ of proper length L lies along the x-axis and moves towards the positive x-direction with speed $v = (3c/5)$ with respect to the ground (see figure), where c is the speed of light in vacuum. An observer on the ground measures the positions of P and Q at different times t_P and t_Q respectively in the ground frame, and finds the difference between them to be $9L/10$. What is the value of $t_Q - t_P$?



(a) $\frac{L}{3c}$ (b) $\frac{L}{5c}$ (c) $\frac{L}{6c}$ (d) $\frac{2L}{3c}$

41. A symmetric top has principle moments of inertia $I_1 = I_2 = \frac{2\alpha}{3}$, $I_3 = 2\alpha$ about a set of principal axes 1, 2, 3 respectively, passing through its centre of mass, where α is a positive constant. There is no force acting on the body and the angular speed of the body about the 3-axis is $\omega_3 = \frac{1}{8}$ rad/s. With what angular frequency in rad/s does the angular velocity vector $\vec{\omega}_1$ precess about the 3-axis ?

(a) 2 (b) 3 (c) 5 (d) 7

42. A particle of mass *m* is free to move on a frictionless horizontal two dimensional (r, θ) plane, and is acted upon by a force $\vec{F} = -\frac{k}{2r^3}\hat{r}$ with *k* being a positive constant. If p_r and p_θ are the generalized momenta corresponding to *r* and θ respectively, then what is the value of $\frac{dp_r}{dt}$?

(a) $\frac{p_\theta^2 - 2mk}{2mr^3}$ (b) $\frac{2p_\theta^2 - mk}{mr^3}$ (c) $\frac{p_\theta^2 - 2mk}{mr^3}$ (d) $\frac{2p_\theta^2 - mk}{2mr^3}$

43. Consider two real function:

$$U(x, y) = xy(x^2 - y^2)$$

$$V(x, y) = ax^4 + by^4 + cx^2y^2 + k$$

where *k* is a real constant and *a*, *b*, *c* are real coefficients. If $U(x, y) + iV(x, y)$ is analytic, then what is the value of $a \times b \times c$?

(a) $\frac{1}{8}$ (b) $\frac{3}{28}$ (c) $\frac{5}{36}$ (d) $\frac{3}{32}$

44. Young's double slit experiment is performed using a beam of C_{60} (fullerene) molecules, each molecule being made up of 60 carbon atoms. When the slit separation is 50 nm, fringes are formed on a screen kept at a distance of 1 m from the slits. Now, the experiment is repeated with C_{70} molecules with a slit separation of 92.5 nm. The kinetic energies of both the beams are the same. The position of the 4^{th} bright fringe for C_{60} will correspond to the n^{th} bright fringe for C_{70}. What is the value of *n* (rounded off to the nearest integer) ?

(a) 5 (b) 6 (c) 7 (d) 8

45. A neutron beam with a wave vector $\vec{k}$ and an energy 20.4 meV diffracts from a crystal with an outgoing wave vector $\vec{k}'$. One of the diffraction peaks is observed for the reciprocal lattice vector $\vec{G}$ of magnitude 3.14 $Å^{-1}$. What is the diffraction angle in degrees (rounded off to the nearest integer) that $\vec{k}$ makes with the plane? (Use mass of neutron = 1.67×10^{-27} Kg)

(a) 15 (b) 30 (c) 45 (d) 60

46. In the first Brillouin zone of a rectangular lattice (lattice constants $a = 6$ A and $b = 4$ A), three incoming phonons with the same wave vector $\langle 1.2\ \text{Å}^{-1},\ 0.6\ \text{Å}^{-1}\rangle$ interact to give one phonon. Which one of the following is the CORRECT wave vector of the resulting phonon?

(a) $\langle 2.56\ \text{Å}^{-1},\ 0.23\ \text{Å}^{-1}\rangle$ (b) $\langle 3.60\ \text{Å}^{-1},\ 1.80\ \text{Å}^{-1}\rangle$

(c) $\langle 0.48\ \text{Å}^{-1},\ 0.23\ \text{Å}^{-1}\rangle$ (d) $\langle 3.60\ \text{Å}^{-1},\ -0.80\ \text{Å}^{-1}\rangle$

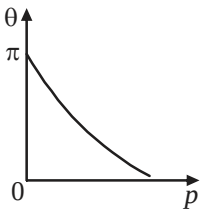
47. For a covalently bonded solid consisting of ions of mass m, the binding potential can be assumed to be given by

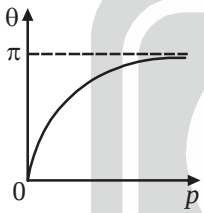
$$U(r) = -\varepsilon\left(\frac{r}{r_0}\right)e^{-r/r_0},$$

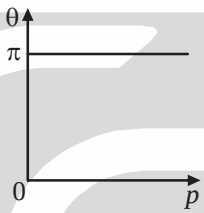
where ε and r_0 positive constants. What is the Einstein frequency of the solid in Hz ?

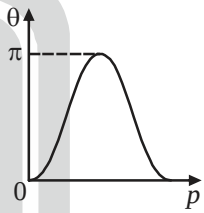
(a) $\dfrac{1}{2\pi}\sqrt{\dfrac{\varepsilon e}{mr_0^2}}$ (b) $\dfrac{1}{2\pi}\sqrt{\dfrac{\varepsilon}{mer_0^2}}$ (c) $\dfrac{1}{2\pi}\sqrt{\dfrac{2\varepsilon}{mer_0^2}}$ (d) $\dfrac{1}{2\pi}\sqrt{\dfrac{\varepsilon e}{2mr_0^2}}$

48. In a hadronic interaction, π^0's are produced with different momenta, and they immediately decay into two photons with an opening angle θ between them. Assuming that all these decays occur in one plane, which one of the following figures depicts the behaviour of θ as a function of the π^0 momentum p ?

(a) 

(b) 

(c) 

(d) 

49. A particle has wavefunction $\psi(x, y, z) = Nze^{-\alpha(x^2+y^2+z^2)}$, where N is a normalization constant and α is a positive constant. In this state, which one of the following options represents the eigenvalues of L^2 and L_z respectively.

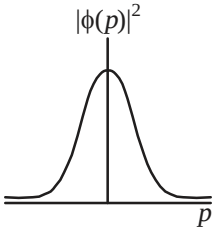
Some values of Y_l^m are: $Y_0^0 = \sqrt{\dfrac{1}{4\pi}},\ Y_1^0 = \sqrt{\dfrac{3}{4\pi}}\cos\theta,\ Y_1^{\pm 1} = \mp\sqrt{\dfrac{3}{8\pi}}\sin\theta e^{\pm i\phi}$

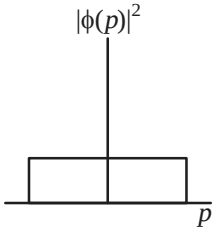
(a) 0 and 0 (b) $\hbar^2$ and $-\hbar$ (c) $2\hbar^2$ and 0 (d) $\hbar^2$ and $\hbar$

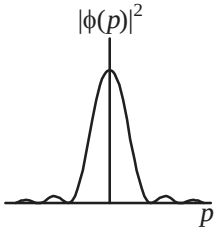
50. The wavefunction of a particle in one dimension is given by:

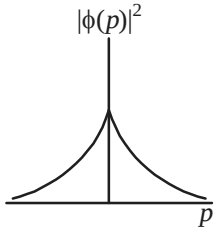
$$\psi(x) = \begin{cases} M & ; \quad -a < x < a \\ 0 & ; \quad \text{otherwise} \end{cases}$$

Here M and a are positive constants. If $\phi(p)$ is the corresponding momentum space wavefunction, which one of the following plots best represents $|\phi(p)|^2$?

(a) 

(b) 

(c) 

(d) 

51. Consider a particle in a two dimensional infinite square well potential of side L, with $0 \le x \le L$ and $0 \le y \le L$. The wavefunction of the particle is zero only along the line $y = (L/2)$, apart from the boundaries of the well. If the energy of the particle in this state is E, what is the energy of the ground state?

(a) $\frac{1}{4}E$ (b) $\frac{2}{5}E$ (c) $\frac{3}{8}E$ (d) $\frac{1}{2}E$

52. Consider two non-identical spin 1/2 particles labelled 1 and 2 in the spin product state $\left|\frac{1}{2}, \frac{1}{2}\right\rangle \left|\frac{1}{2}, -\frac{1}{2}\right\rangle$. The Hamiltonian of the system is $H = \frac{4\lambda}{\hbar^2}\vec{S}_1 \cdot \vec{S}_2$, where $\vec{S}_1$ and $\vec{S}_2$ are the spin operators of particles 1 and 2, respectively, and λ is a constant with appropriate dimensions. What is the expectation value of H in the above state?

(a) $-\lambda$ (b) -2λ (c) λ (d) 2λ

53. A spin 1/2 particle is in a spin up state along the x-axis (with unit vector $\hat{x}$) and is denoted as $\left|\frac{1}{2}, \frac{1}{2}\right\rangle x$. What is the probability of finding the particle to be in a spin up state along the direction $\hat{x}'$, which lies in the xy-plane and makes an angle θ with respect to the positive x-axis, if such a measurement is made?

(a) $\frac{1}{2}\cos^2\frac{\theta}{4}$ (b) $\cos^2\frac{\theta}{4}$ (c) $\frac{1}{2}\cos^2\frac{\theta}{2}$ (d) $\cos^2\frac{\theta}{2}$

54. Different spectral lines of the Balmer series (transitions $n \to 2$, with n being the principal quantum number) fall one at a time on a Young's double slit apparatus. The separation between the slits is d and the screen is placed at a constant distance from the slits. What factor should d be multiplied by to maintain a constant fringe width for various lines, as n takes different allowed values?

(a) $\frac{n^2-4}{4n^2}$ (b) $\frac{n^2+4}{4n^2}$ (c) $\frac{4n^2}{n^2-4}$ (d) $\frac{4n^2}{n^2+4}$

55. Under parity and time reversal transformations, which of the following statements is(are) TRUE about the electric dipole moment p and the magnetic dipole moment μ ?

(a) p is odd under parity and μ is odd under time reversal.
(b) p is odd under parity and μ is even under time reversal.
(c) p is even under parity and μ is odd under time reversal.
(d) p is even under parity and μ is even under time reversal.

56. Consider the complex function:

$$f(z) = \frac{z^2 \sin z}{(z-\pi)^4}$$

At $z = \pi$, which of the following options is(are) CORRECT?

(a) The order of the pole is 4. (b) The order of the pole is 3.
(c) The residue at the pole is $\pi/6$. (d) The residue at the is $2\pi/3$.

57. Consider the vector field $\vec{V}$ consisting of the velocities of points on a thin horizontal disc of radius $R = 2$ m, moving anticlockwise with uniform angular speed $\omega = 2$ rad/sec about an axis passing through its center. If $V = |\vec{V}|$, then which of the following options is(are) CORRECT ? (In the options, $\hat{r}$ and $\hat{\theta}$ are unit vectors corresponding to the plane polar coordinates r and θ).

You may use the fact that in cylindrical coordinates (s, ϕ, z) (s is the distance from the z-axis), the gradient, divergence, curl and Laplacian operators are:

$$\vec{\nabla} f = \frac{\partial f}{\partial s}\hat{s} + \frac{1}{s}\frac{\partial f}{\partial \phi}\hat{\phi} + \frac{\partial f}{\partial z}\hat{z}; \qquad \vec{\nabla}\cdot\vec{A} = \frac{1}{s}\frac{\partial}{\partial s}(sA_s) + \frac{1}{s}\frac{\partial A_\phi}{\partial \phi} + \frac{\partial A_z}{\partial z};$$

$$\vec{\nabla}\times\vec{A} = \left(\frac{1}{s}\frac{\partial A_z}{\partial \phi} - \frac{\partial A_\phi}{\partial z}\right)\hat{s} + \left(\frac{\partial A_s}{\partial z} - \frac{\partial A_z}{\partial s}\right)\hat{\phi} + \frac{1}{s}\left(\frac{\partial}{\partial s}(sA_\phi) - \frac{\partial A_s}{\partial \phi}\right)\hat{z};$$

$$\vec{\nabla}^2 f = \frac{1}{s}\frac{\partial}{\partial s}\left(s\frac{\partial f}{\partial s}\right) + \frac{1}{s^2}\frac{\partial^2 f}{\partial \phi^2} + \frac{\partial^2 f}{\partial z^2}.$$

(a) $\vec{\nabla} V = 2\hat{r}$ (b) $\vec{\nabla}\cdot\vec{V} = 2$

(c) $\vec{\nabla}\times\vec{V} = 4\hat{z}$, where $\hat{z}$ is a unit vector perpendicular to the (r, θ) plane

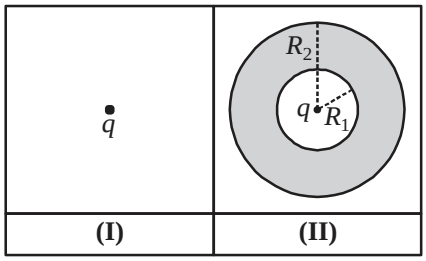
(d) $\vec{\nabla}^2 V = \frac{4}{3}$ at $r = 1.5$ m

58. A slow moving π^- particle is captured by a deuteron (d) and this reaction produces two neutrons (n) in the final state, i.e., $\pi^- + d \to n + n$. Neutron and deuteron have even intrinsic parities, whereas π^- has odd intrinsic parity. L and S are the orbital and spin angular momenta, respectively of the system of two neutrons. Which of the following statements regarding the final two-neutron state is(are) CORRECT?

(a) It has odd parity (b) $L + S$ is odd (c) $L = 1, S = 1$ (d) $L = 2, S = 0$

59. Two independent electrostatic configurations are shown in the figure. Configuration (*I*) consists of an isolated point charge $q = 1$ C, and configuration (*II*) consists of another identical charge surrounded by a thick conducting shell of inner radius $R_1 = 1$ m and outer radius $R_2 = 2$ m, with the charge being at the center of the shell.

$W_I = \frac{\varepsilon_0}{2}\int E_I^2\, dV$ and $W_{II} = \frac{\varepsilon_0}{2}\int E_{II}^2\, dV$, where E_I and E_{II} are the magnitudes of the electric fields for configurations (*I*) and (*II*) respectively, ε_0 is the permittivity of vacuum, and the volume integrations are carried out over all space. If $8\pi\varepsilon_0 |W_I - W_{II}| = \frac{1}{n}$, what is the value of the integer n ?



60. In pion nucleon scattering, the pion and nucleon can combine to form a short lived bound state called the Δ particle $(\pi + N \rightarrow \Delta)$. The masses of the pion, nucleon and the Δ particle are 140 MeV/c^2, 938 MeV/c^2 and 1230 MeV/c^2, respectively. In this lab frame, where the nucleon is at rest, what is the minimum energy (in MeV/c^2, rounded off to one decimal place) of the pion to produce the Δ particle ?

61. Consider an electromagnetic wave propagating in the *z*-direction in vacuum, with the magnetic field given by $\vec{B} = \vec{B}_0 e^{i(kz-\omega t)}$. If $B_0 = 10^{-8}$ T, the average power passing through a circle of radius 1.0 m placed in the *xy*-plane is *P* (in Watts). Using $\varepsilon_0 = 10^{-11}\dfrac{c^2}{\text{Nm}^2}$, what is the value of $\dfrac{10^3 P}{\pi}$ (rounded off to one decimal place)?

62. An α -particle is emitted from the decay of Americium (Am) at rest, i.e., ${}^{241}_{94}\text{Am} \rightarrow {}^{237}_{92}\text{U} + \alpha$. The rest masses of ${}^{241}_{94}\text{Am}$, ${}^{237}_{92}\text{U}$ and α are 224.544 GeV/c^2, 220.811 GeV/c^2 and 3.728 GeV/c^2 respectively. What is the kinetic energy (in MeV/c^2, rounded off to two decimal places) of the α -particle?

63. Consider 6 identical, non-interacting, spin 1/2 atoms arranged on a crystal lattice at absolute temperature *T*. The *z*-component of the magnetic moment of each of these atoms can be $\pm \mu_B$. If *P* and *Q* are the probabilities of the net magnetic moment of the solid being $2\mu_B$ and $6\mu_B$ respectively, what is the value of P/Q (in integer)?

64. Two identical, non-interacting $^4\text{He}_2$ atoms are distributed among 4 different non-degenerate energy levels. The probability that they occupy different energy levels is *p*. Similarly, two $^3\text{He}_2$ atoms are distributed among 4 different non-degenerate energy levels, and the probability that they occupy different levels is *q*. What is the value of *p*/*q* (Rounded off to one decimal place)?

65. Two identical bodies kept at temperatures 800 K and 200 K act as the hot and the cold reservoirs of an ideal heat engine, respectively. Assume that their heat capacity (*C*) in Joules/K is independent of temperature and that they do not undergo any phase change. Then, the maximum work that can be obtained from the heat engine is $n \times C$ Joules. What is the value of *n* (in integer)?

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